

# Thermoelectrics 101

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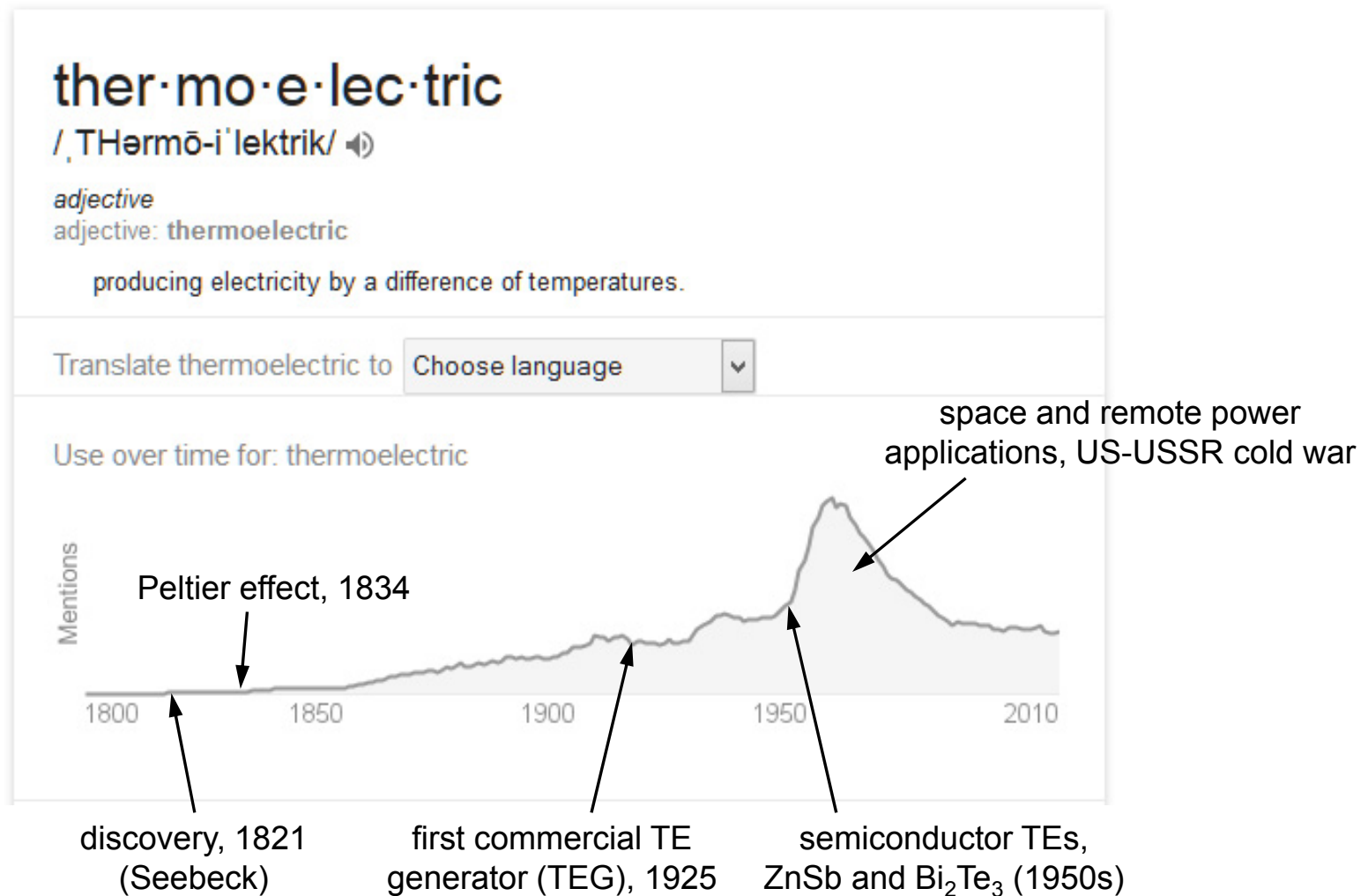
# Outline

## **1) Fundamentals**

## 2) Applications

## 3) Final Remarks

# Definition and Usage

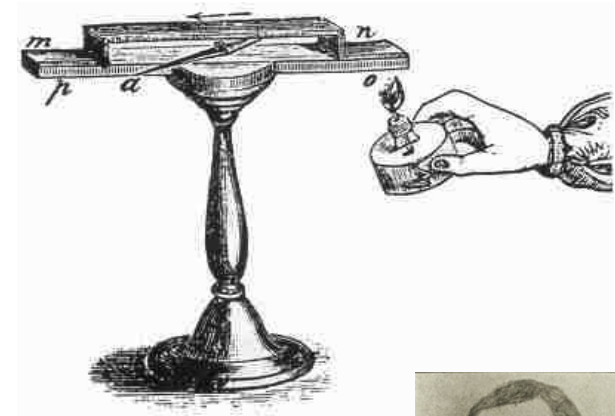


# Seebeck vs. Peltier

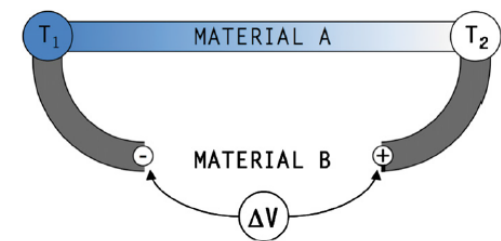
- Seebeck effect (1821):
  - Loop of Cu and Bi wires (thermocouple)
  - Heating one end deflected magnetic needle, initial confused with thermomagnetism
  - Ørsted (1823) correctly explained that **electric flow occurred due to temperature gradient**

$$\Delta V \equiv (S_B - S_A)\Delta T$$

- $S_{A,B}$  = Seebeck coefficient = thermopower specific to material A or B (units of  $\mu\text{V/K}$ )
- Ex:  $\Delta S \sim 300 \mu\text{V/K}$  and  $\Delta T = 100 \text{ K}$ , we generate 30 mV
- *Q: how do we generate 1.5 V like AA battery?*



Thomas Seebeck





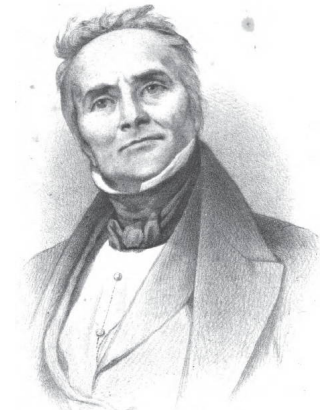
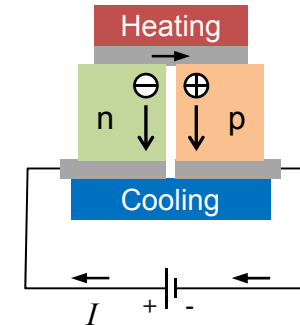
# Seebeck vs. Peltier

- Peltier effect (1834):

- Opposite of Seebeck effect
- **Electric current flow through a junction of materials A and B can be used to heat or cool**

$$Q \equiv \Pi_{AB} I = (S_B - S_A) T I$$

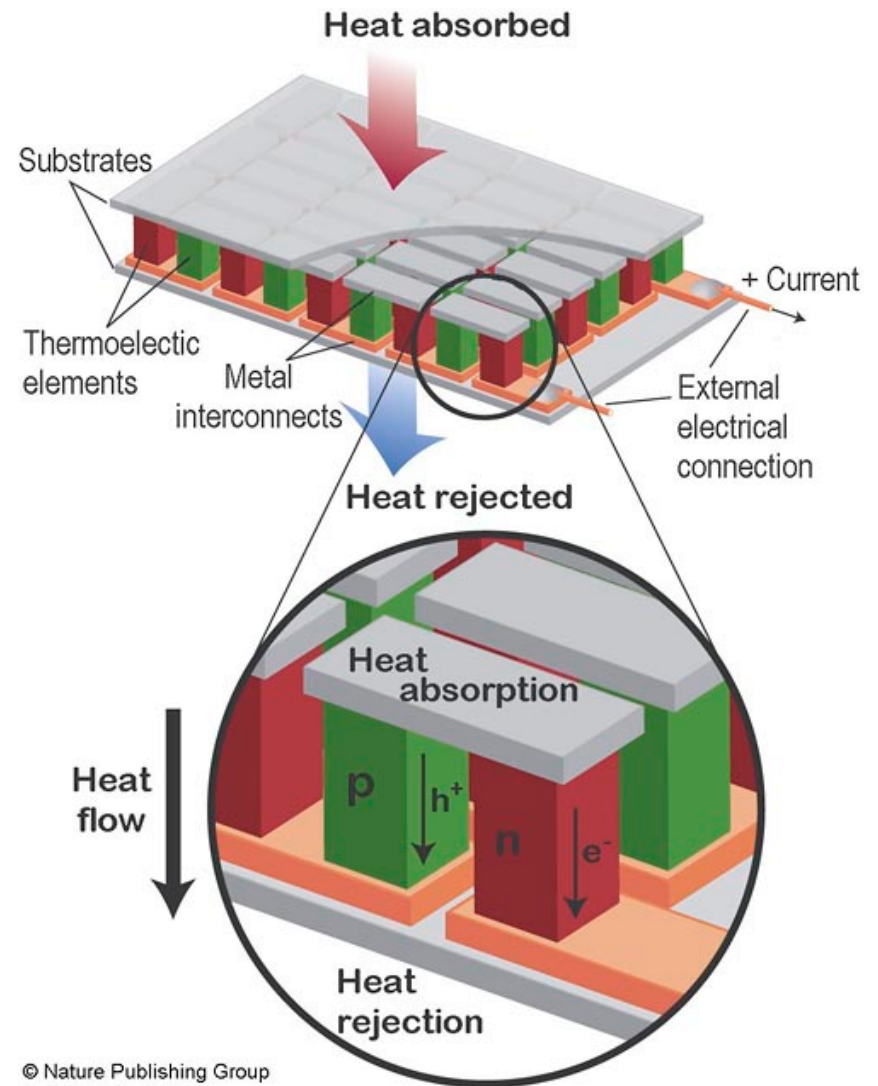
- $\Pi_{AB} = S_{AB} T$  = Peltier coefficient of junction
- Heating and cooling are reversible, depending on the direction ( $\pm$  sign) of the current  $I$
- Ex:  $I = 1 \text{ mA}$ ,  $\Delta S \sim 300 \text{ } \mu\text{V/K}$  and  $T = 300 \text{ K}$  gives us cooling power of  $90 \text{ } \mu\text{W}$
- *Q: how do we generate greater cooling (or heating) power?*



Jean Peltier

# Answer (Look Ahead)

- Commercial TE modules are typically arranged in a series of alternating “n” and “p”-doped semiconductor legs
- TE legs are “electrically in series” and “thermally in parallel”



# Seebeck vs. Peltier vs. Thomson Effect

- Thomson effect (1851):

- *Continuous* version of Seebeck effect, no junction needed
- Gradual change in  $S$  ( $\nabla S$ ) due to temperature variation ( $\nabla T$ ) inside a material creates local electric field ( $\nabla V$ ) and local heating or cooling ( $Q$ )

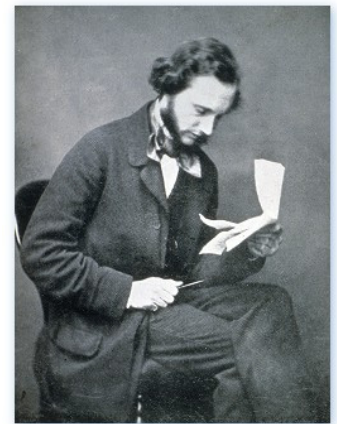
$$\nabla V = T \nabla S$$

$$Q = T \mathbf{J} \cdot \nabla S$$

current density  
(A/m<sup>2</sup>)



- Thomson effect directly measurable in one material
- Peltier and Seebeck more easily measurable for pairs of materials
- Seebeck, Peltier, Thomson effects are *reversible*
- Joule heating ( $I^2R$ ) is *not* reversible



William Thomson  
(Lord Kelvin)

# Combining TE, Joule & Heat Flow

- Electric field:

$$\mathbf{E} = -\nabla V = \underbrace{\frac{\mathbf{J}}{\sigma}}_{\text{Ohm}} + \underbrace{S\nabla T}_{\text{Seebeck}}$$

- Heat flux:

$$Q'' = -k\nabla T + STJ$$

- Local current density:

$$\mathbf{J} = \sigma(-\nabla V - S\nabla T)$$

- Heat diffusion equation with Seebeck effects and Joule heating

$$-Q''' = \nabla \cdot (k\nabla T) + \mathbf{J} \cdot \mathbf{E} - T\mathbf{J} \cdot \nabla S$$

# Common Seebeck Coefficients

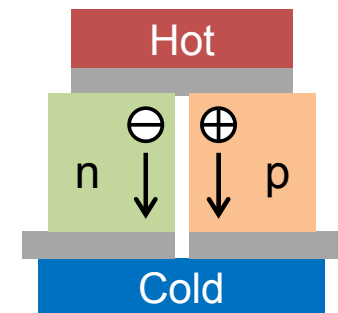
Material	Seebeck coefficient S relative to platinum ( $\mu\text{V/K}$ )	
<a href="#">Selenium</a>	900	} semiconductors tend to have high $ S $ , but magnitude and sign depend on doping ( $S_p > 0$ and $S_n < 0$ )
<a href="#">Tellurium</a>	500	
<a href="#">Silicon</a>	440	
<a href="#">Germanium</a>	330	
<a href="#">Antimony</a>	47	
<a href="#">Nichrome</a>	25	} metals tend to have low S
<a href="#">Molybdenum</a>	10	
<a href="#">Cadmium, tungsten</a>	7.5	
<a href="#">Gold, silver, copper</a>	6.5	
<a href="#">Rhodium</a>	6.0	
<a href="#">Tantalum</a>	4.5	
<a href="#">Lead</a>	4.0	
<a href="#">Aluminium</a>	3.5	
<a href="#">Carbon</a>	3.0	
<a href="#">Mercury</a>	0.6	
<a href="#">Platinum</a>	0 (definition)	
<a href="#">Sodium</a>	-2.0	
<a href="#">Potassium</a>	-9.0	
<a href="#">Nickel</a>	-15	
<a href="#">Constantan</a>	-35	
<a href="#">Bismuth</a>	-72	

Thomas Seebeck's original junction

source: Wikipedia

# What Is the Microscopic Origin of TE?

- Seebeck = electrons (or holes\*) diffuse in a temperature gradient, leading to  $\Delta V$ 
  - Diffusion from hot to cold  $\rightarrow$  like hot air molecules ( $O_2$ ,  $N_2$ ) diffusing from space heater to farthest corners of the room
  - Kinetic energy  $\rightarrow (3/2)k_B T \approx (1/2)mv^2 \rightarrow v = (3k_B T/m)^{1/2}$
  - Hotter electrons (or holes) are faster, but they also carry charge, which sets up the voltage gradient
- Peltier = electrons (or holes\*) carry kinetic energy (in addition to charge) as they move with current flow
  - Explains why we prefer materials with higher  $\sigma$  (electrical conductivity), i.e. metals or highly doped semiconductors



\*hole = missing electron in a material = broken bond

# Seebeck Coefficient (Classical & Metals)

- Seebeck coefficient can be thought of as the heat per carrier per degree K (specific heat per carrier),  $S \approx C/q$
- In classical electron gas (recall  $k_B/q = 86 \mu\text{V/K}$ ):

$$S_{\text{classic}} \approx \frac{3}{2} \frac{k_B}{q} \approx 130 \mu\text{V/K}$$

- In normal metals only small fraction around  $E_F$  contribute, so the thermopower is very small:

$$S_{\text{metal}} \approx \left( \frac{k_B T}{E_F} \right) \frac{k_B}{q} \approx 1 \mu\text{V/K}$$

- In semiconductors, energy carriers can be “far” from  $E_F$ , so the thermopower can be large:

$$S_{\text{semi}} \approx \left| \frac{E - E_F}{qT} \right| \approx 1 \text{ mV/K}$$

# Seebeck Coefficient (In General)

- Keeping track of particle motion (Boltzmann transport equation)

$$\mathbf{v} \cdot \nabla_{\mathbf{r}} f + \frac{q\mathbf{F}}{\hbar} \cdot \nabla_{\mathbf{k}} f = -\frac{f(\mathbf{r}, \mathbf{k}) - f_{\text{eq}}(\mathbf{r}, \mathbf{k})}{\tau(\mathbf{k})}$$

- Where

$$f_{\text{eq}} = \frac{1}{1 + \exp \frac{E - E_F}{k_B T}}$$

- The electrical conductivity and Seebeck coefficient are:


$$\sigma = \int \sigma(E) dE$$

$$S = \frac{1}{qT} \frac{\int (E - E_F) \sigma(E) dE}{\int \sigma(E) dE}$$

- Where the *differential* conductivity

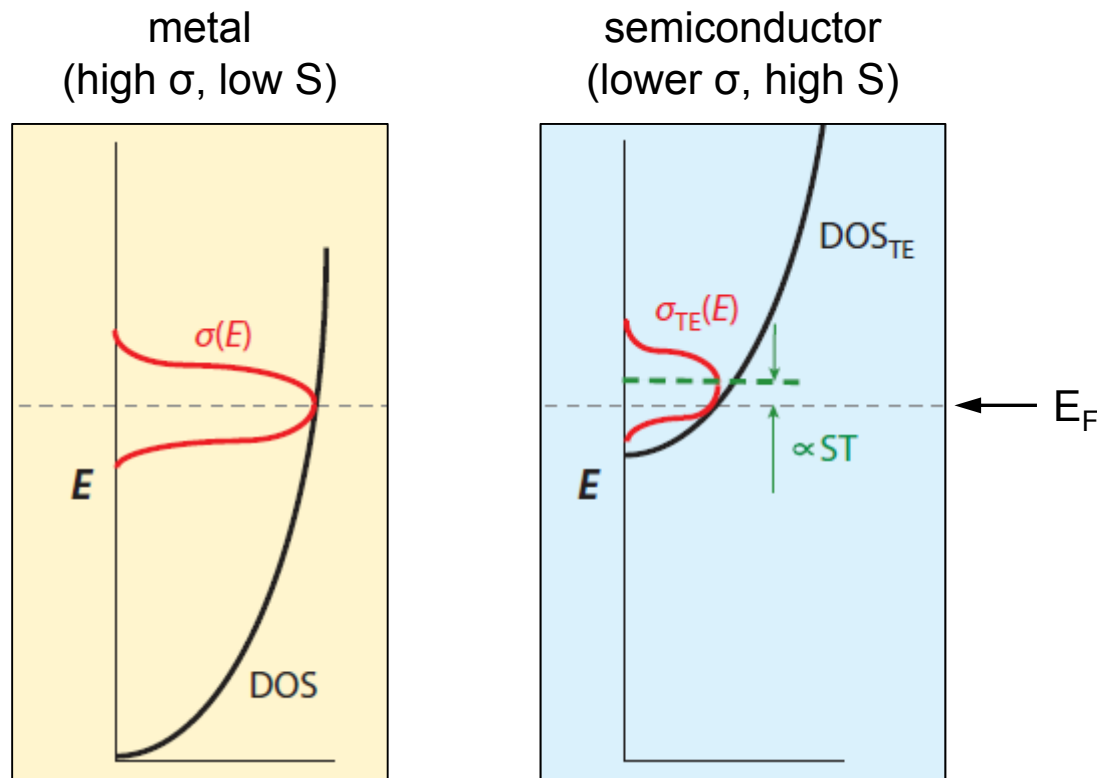
$$\sigma(E) = q^2 \tau(E) v^2(E) D(E) \left( -\frac{\partial f_{\text{eq}}}{\partial E} \right)$$

density of states (DOS)





# Picturing the Transport “Window”

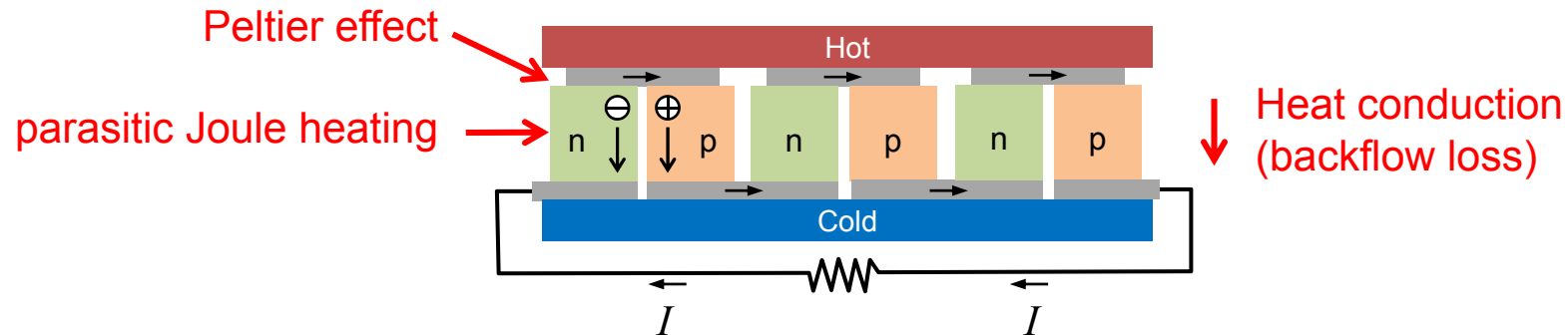


- In metals, density of states (DOS) does not vary sharply around  $E_F$
- In doped semiconductors,  $E_F$  is at band edge where DOS varies sharply (ex: in  $n$ -type semiconductor, more states available for transport above than below  $E_F$ ) → **for high  $S$ , need asymmetric DOS near  $E_F$**

Shakouri, *Annu. Rev. Mater. Res.* (2011)

# Thermoelectric Figure of Merit (ZT)

- How efficient are TEs?



Obtain highest

$$Q = STI - I^2 \left( \frac{L}{\sigma A} \right) - \frac{kA\Delta T}{L}$$

Peltier

Joule loss

Heat backflow

When maximizing

$$ZT = \frac{S^2 \sigma T}{k}$$

$\leftarrow k_e + k_L$

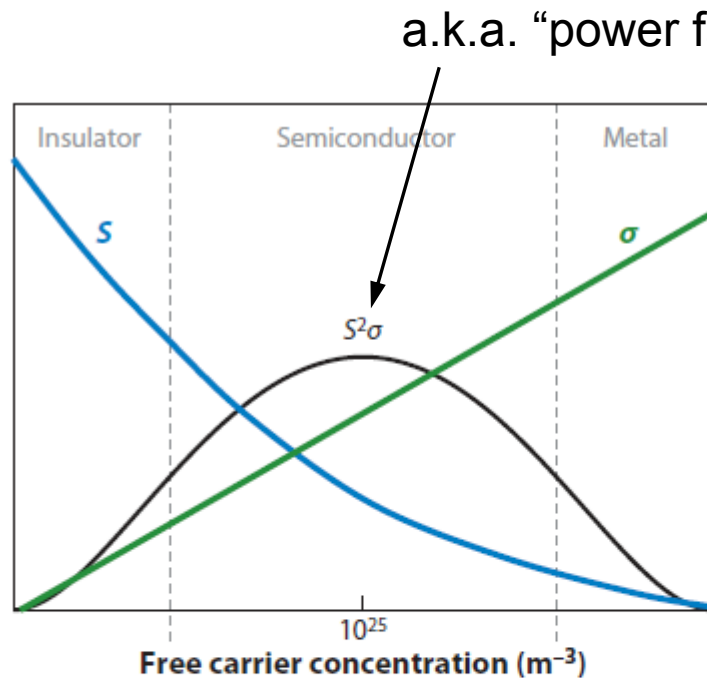
# Thermoelectric Figure of Merit (ZT)

- How efficient are TEs?
- Figure of merit:

$$ZT = \frac{S^2 \sigma T}{k} \longleftarrow k_e + k_L$$

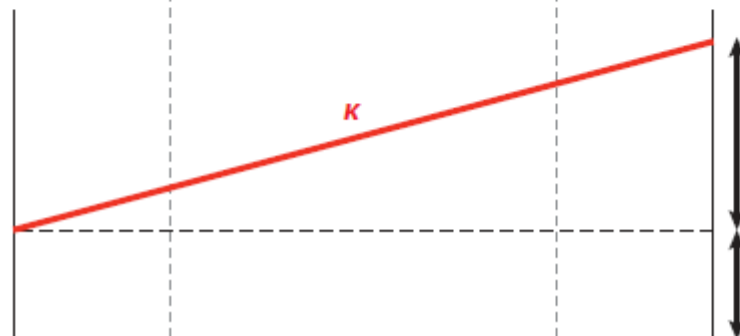
- Thus, **one must simultaneously maximize S and  $\sigma$  (electrical conductivity) while minimizing k (thermal conductivity)**
- These quantities are inter-related, such that increasing S typically leads to decreasing  $\sigma$
- Also,  $k = k_e + k_L$ , thermal conductivity is sum of electron and lattice (phonon) contributions, so increasing  $\sigma$  leads to increasing  $k_e \leftrightarrow$  Wiedemann-Franz-Lorenz (WFL) law

# Trade-Offs in Maximizing ZT



Interesting: if  $k_L = 0$  (hypothetically)  
then  $(ZT)_{\max} = S^2/L_0$

Ex: if  $S = 300 \mu\text{V/K}$  then  $(ZT)_{\max} = 3.7$



Electronic  
contribution

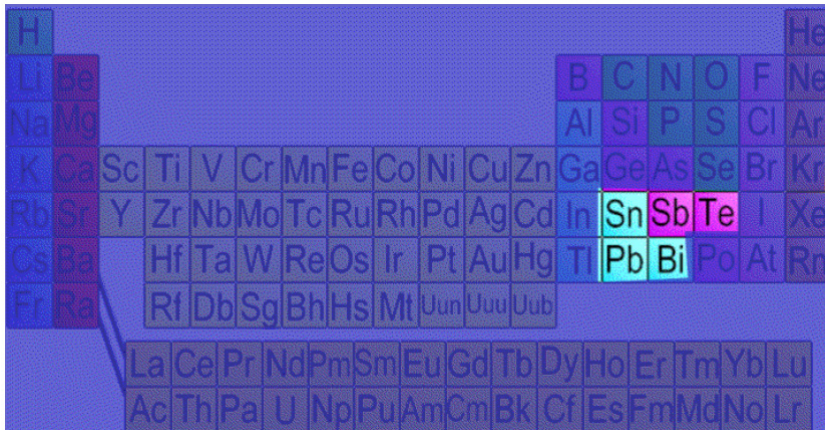
$$k_e = L_0 T \sigma \quad (\text{WFL})$$

Lattice  
contribution

$k_L$  must be minimized

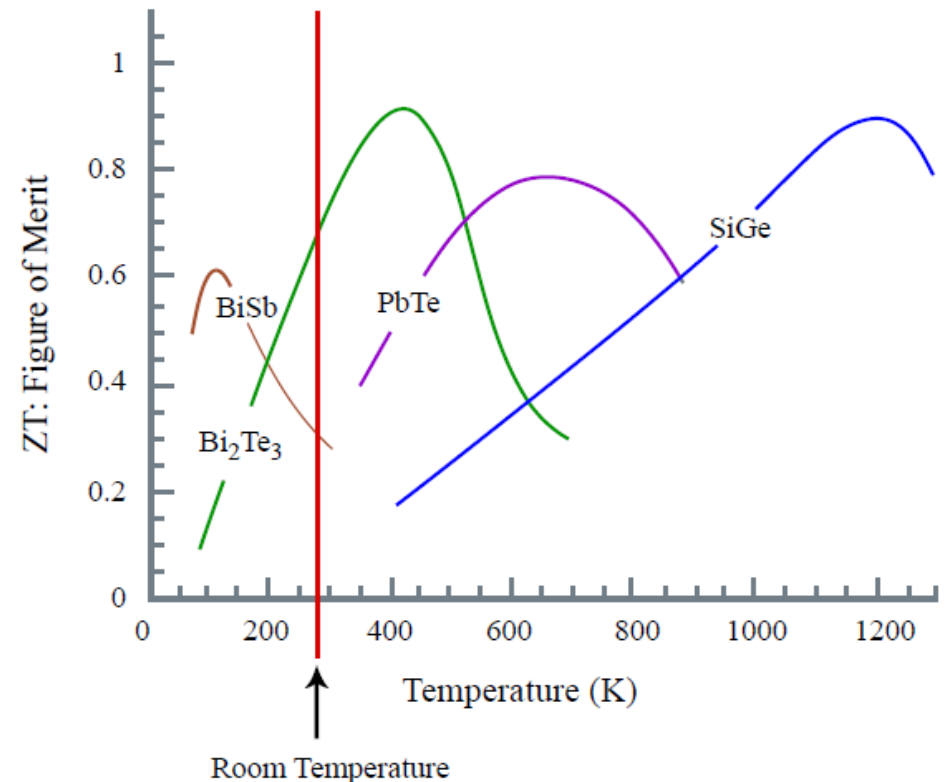
Lorenz constant  $L_0 = 2.45 \times 10^{-8} \text{ W}\Omega/\text{K}^2$

# ZT for Commercial Materials



H																	He
Li	Be											B	C	N	O	F	Ne
Na	Mg											Al	Si	P	S	Cl	Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba		Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
Fr	Ra		Rf	Db	Sg	Bh	Hs	Mt	Uun	Uuu	Uub						
		La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu	
		Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr	

- $0.6 < ZT < 1$  for commercially available materials over 300-1200 K temperature range
- Note different materials are best at different temperatures

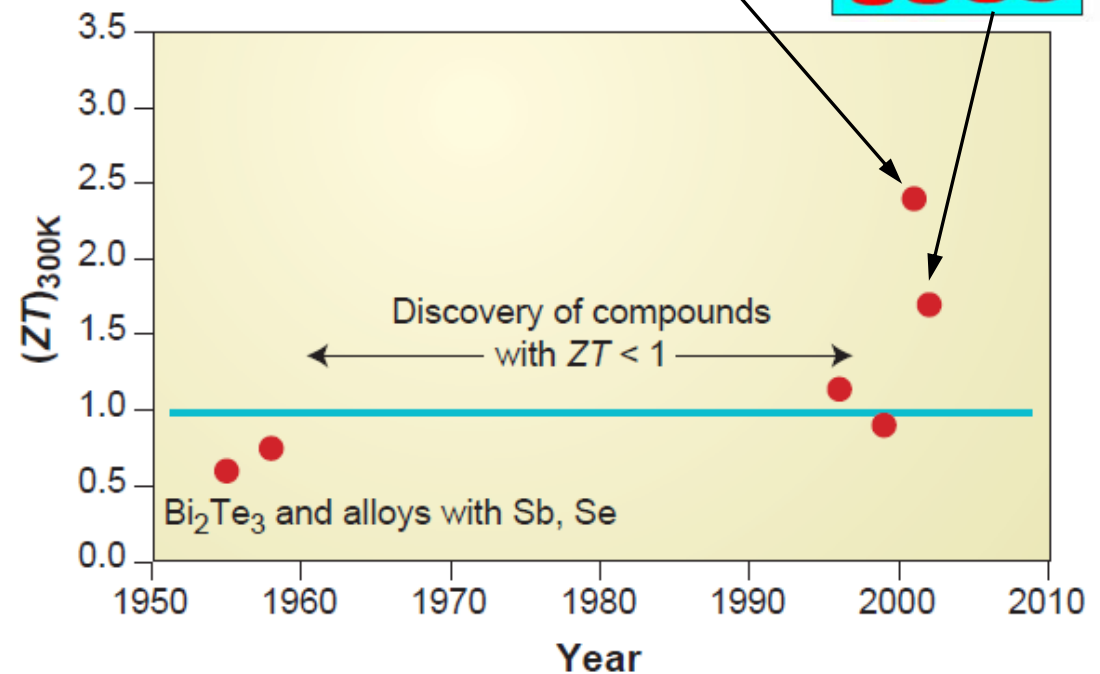
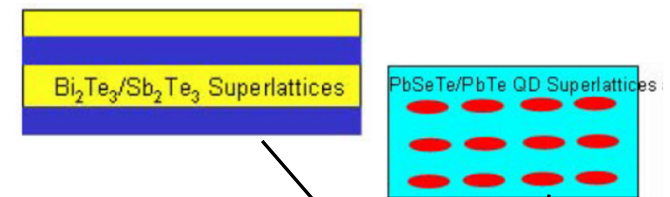


# Evolution of ZT over Time

Over ~5 decades ZT has been limited to  $\leq 1$  (at room temperature)

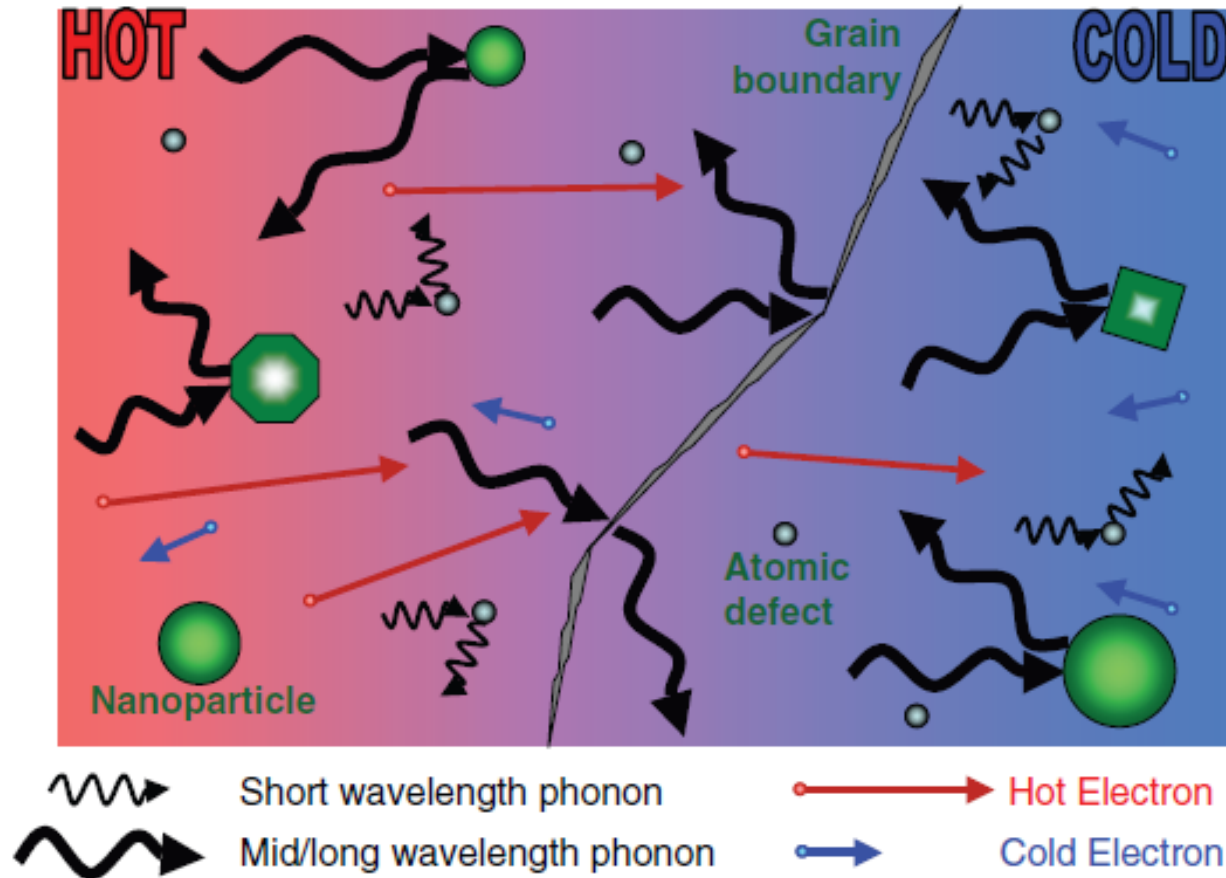
Improvements have often come from artificially lowering thermal  $k_L$

Exploiting nanostructuring and superlattices



Source: A. Majumdar, *Science* (2004)

# How Can We Lower Thermal K?



- Introduce features that scatter phonons, not electrons
- “Phonon glass, electron crystal” (G. Slack, 1960s)

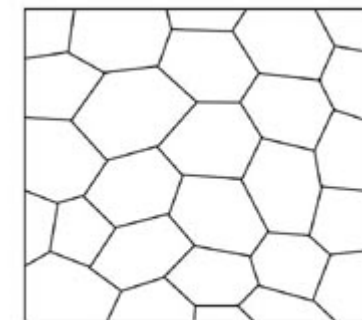
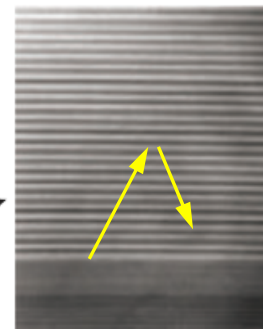
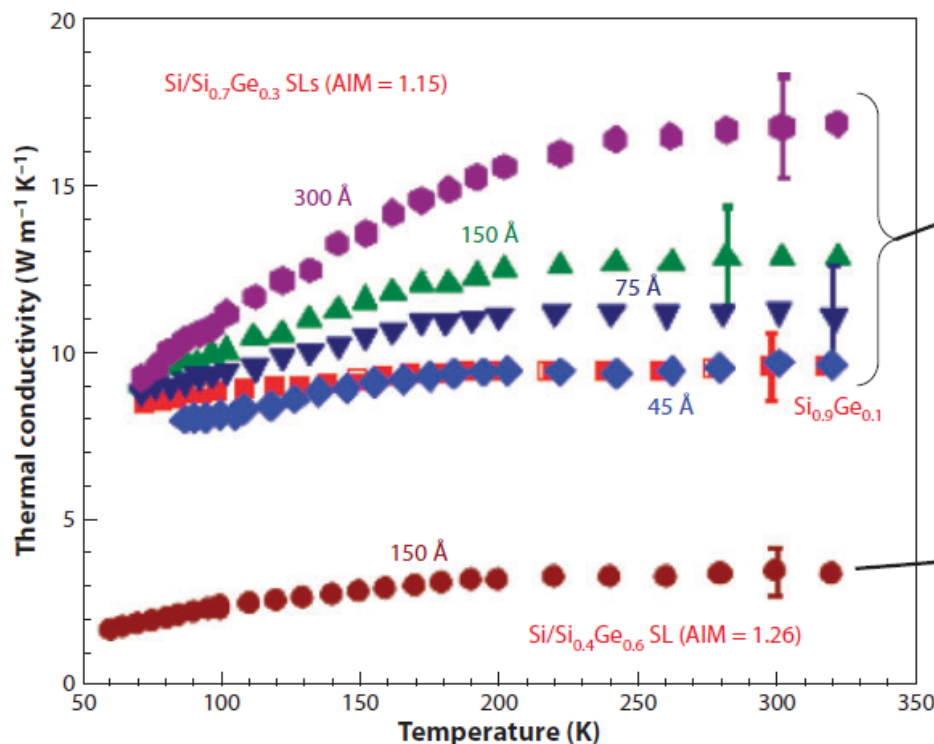


# Reducing Thermal Conductivity

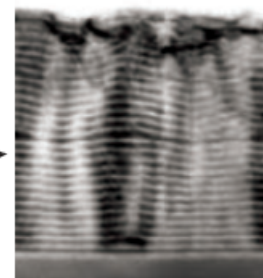
- Reduce thermal  $k_L$  using nanoscale scattering features

$$k_L = \frac{1}{3} C v \lambda$$

reduce mean free path by  
increasing number of interfaces



Small Grain



Lamella within Grains



# Reducing Thermal Conductivity

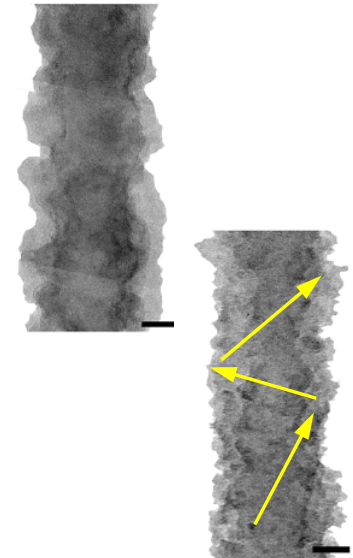
- Using edge roughness of Si nanowires

Vol 451 | 10 January 2008 | doi:10.1038/nature06381

nature

## Enhanced thermoelectric performance of rough silicon nanowires

Allon I. Hochbaum<sup>1\*</sup>, Renkun Chen<sup>2\*</sup>, Raul Diaz Delgado<sup>1</sup>, Wenjie Liang<sup>1</sup>, Erik C. Garnett<sup>1</sup>, Mark Najarian<sup>3</sup>, Arun Majumdar<sup>2,3,4</sup> & Peidong Yang<sup>1,3,4</sup>



PRL 102, 125503 (2009)

PHYSICAL REVIEW LETTERS

week ending  
27 MARCH 2009



### Impact of Phonon-Surface Roughness Scattering on Thermal Conductivity of Thin Si Nanowires

Pierre Martin,<sup>1,\*</sup> Zlatan Aksamija,<sup>1</sup> Eric Pop,<sup>1,2,†</sup> and Umberto Ravaioli<sup>1</sup>

<sup>1</sup>Beckman Institute and Department of Electrical and Computer Engineering, University of Illinois, Urbana-Champaign, Urbana, Illinois 61801, USA

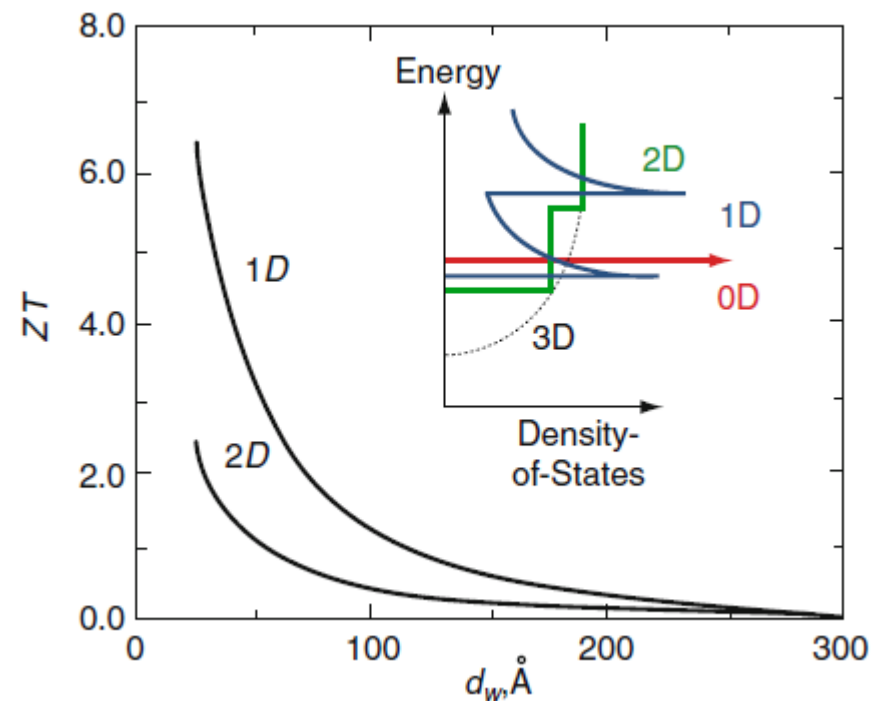
<sup>2</sup>Micro- and Nano-Technology Laboratory, University of Illinois, Urbana-Champaign, Urbana, Illinois 61801, USA

(Received 24 November 2008; published 27 March 2009)

We present a novel approach for computing the surface roughness-limited thermal conductivity of silicon nanowires with diameter  $D < 100$  nm. A frequency-dependent phonon scattering rate is computed from perturbation theory and related to a description of the surface through the root-mean-square roughness height  $\Delta$  and autocovariance length  $L$ . Using a full phonon dispersion relation, we find a quadratic dependence of thermal conductivity on diameter and roughness as  $(D/\Delta)^2$ . Computed results show excellent agreement with experimental data for a wide diameter and temperature range (25–350 K),

# Effects of Nanostructuring on TEs

- Hicks and Dresselhaus (1993)\* pioneered concept of quantum confinement effects for TEs
- Sharp features in the 1D and 2D density of states (DOS) lead to asymmetric  $\sigma(E)$  and should increase  $S$
- Challenge: sharp DOS features become “blurred” if there is size non-uniformity in the system
- Most recent breakthroughs benefitted from reduction in  $k_L$



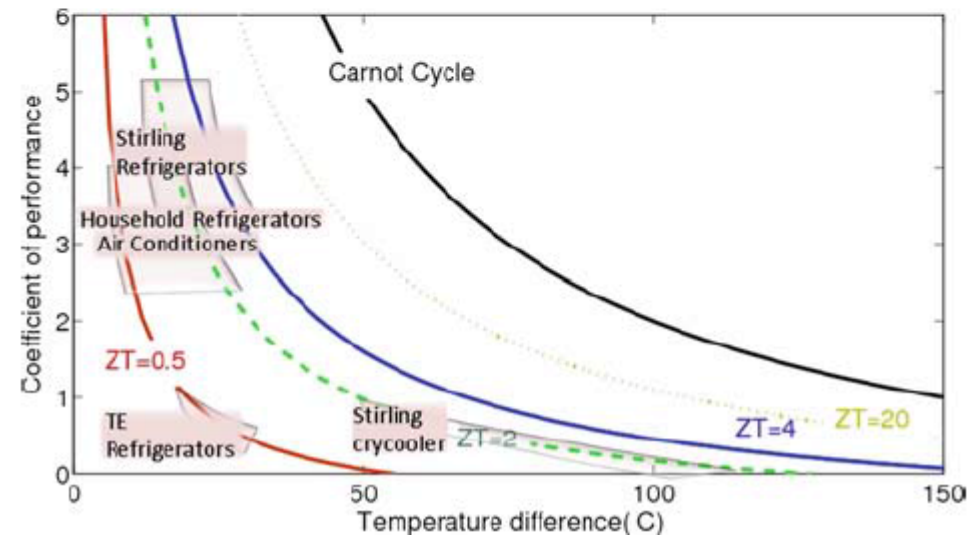
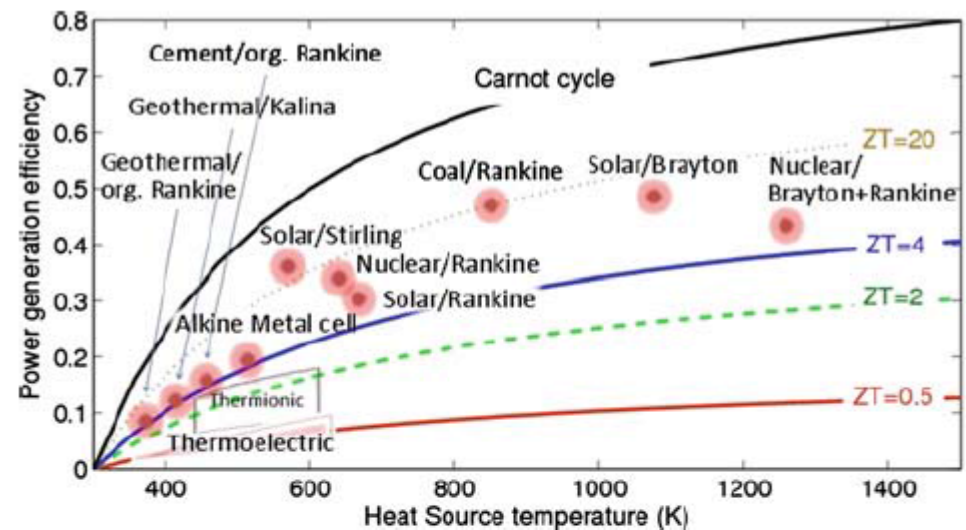
\*<http://dx.doi.org/10.1103/PhysRevB.47.12727>

# How High ZT?

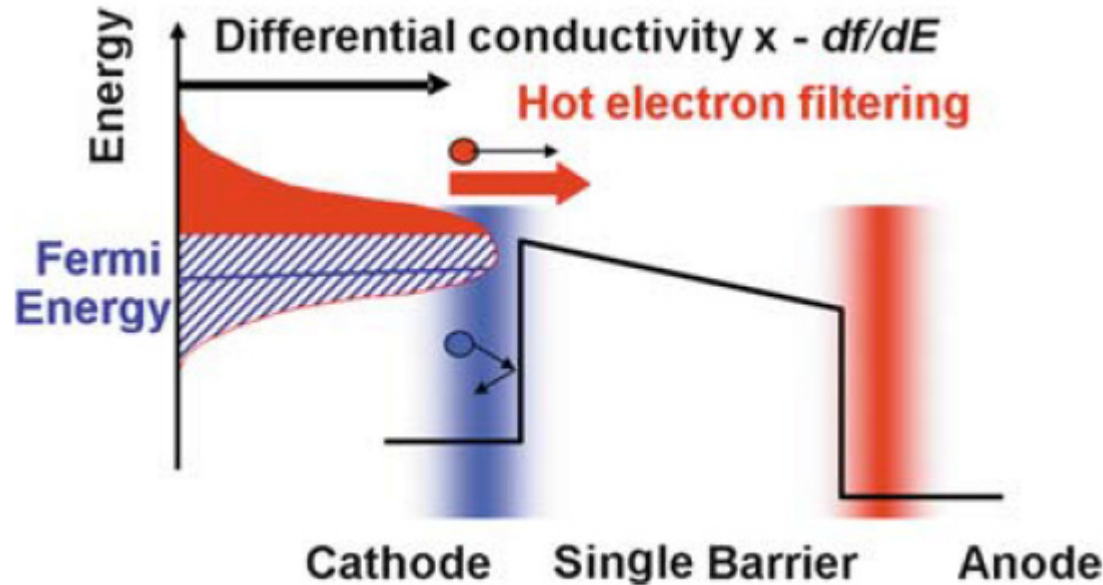
- TE efficiency

$$\eta = \frac{\Delta T}{T_h} \cdot \frac{\sqrt{1+ZT} - 1}{\sqrt{1+ZT} + T_c/T_h}$$

- Cooling** comparison: modern (mechanical) refrigerator efficiency equivalent to  $ZT \sim 3$
- Power generation** comparison: steam power plants are ~40% efficient



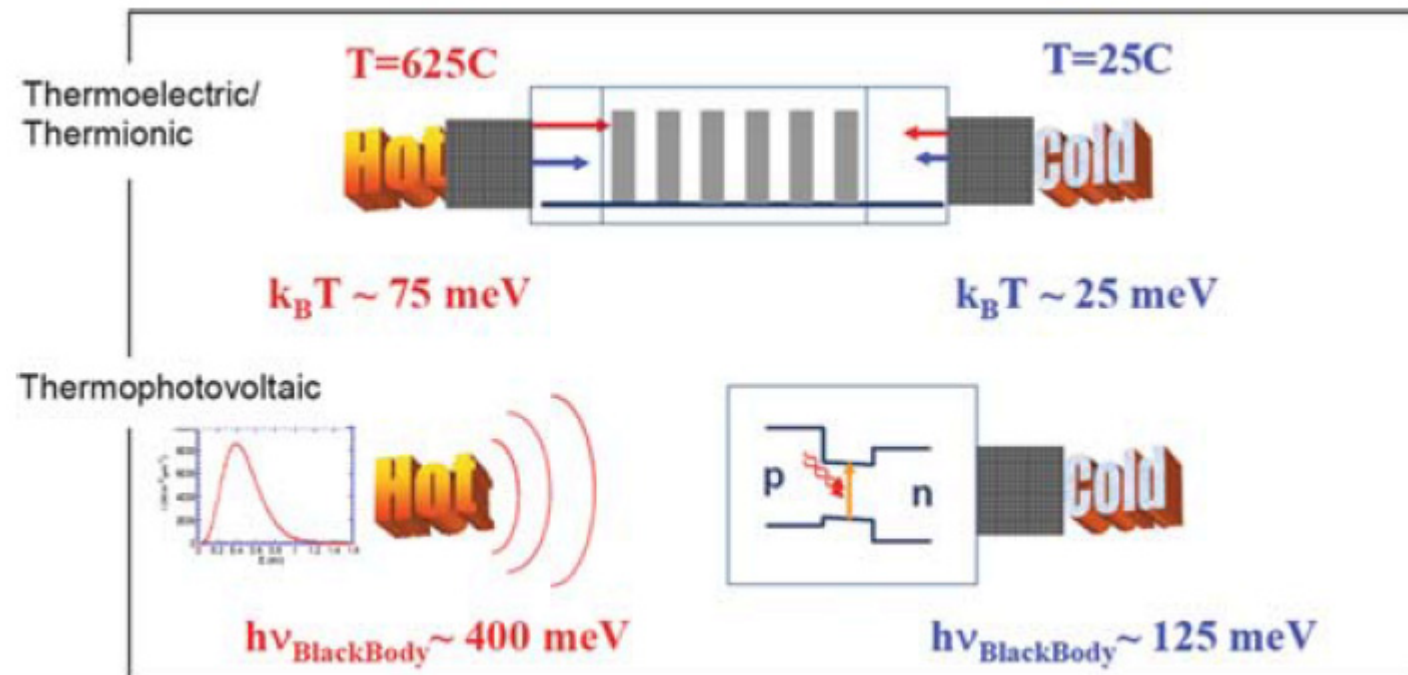
# Alternative: Thermionic (TI) Energy Conversion



- Design tunnel barrier that blocks (filters out) the cold electron distribution, to obtain maximum energy transmission
- Nanoscale vacuum gap is best electron (tunneling) conductor and worst thermal (phonon) conductor
- Challenges in controlling uniform tunnel gaps and efficiency only at higher temperatures

source: Shakouri (2010)

# Alternative: Thermophotovoltaics (TPV)



- Filter peak emission of thermal radiation from hot source
- Transmitted photons converted to electron-hole pairs in pn junction
  - TPV avoids some losses of conventional PV and heat backflow problem of TE
  - However, must avoid non-radiative recombination in pn junction

# Questions?

# Outline

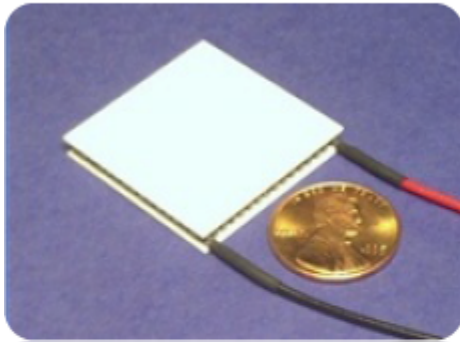
1) Fundamentals

**2) Applications**

3) Final Remarks

# Thermoelectric Applications

## Electric Cooling

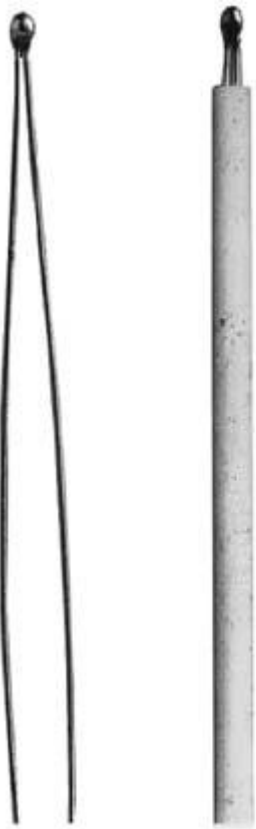


## Power Generation

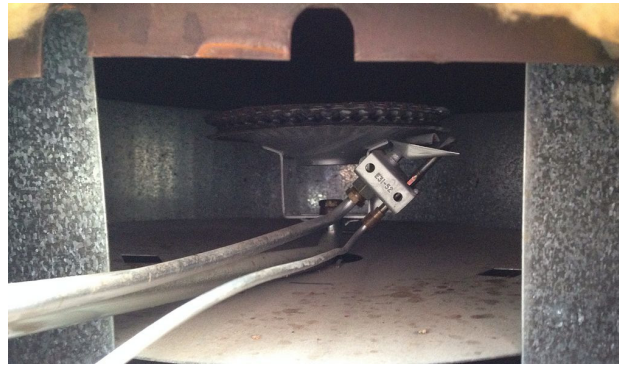




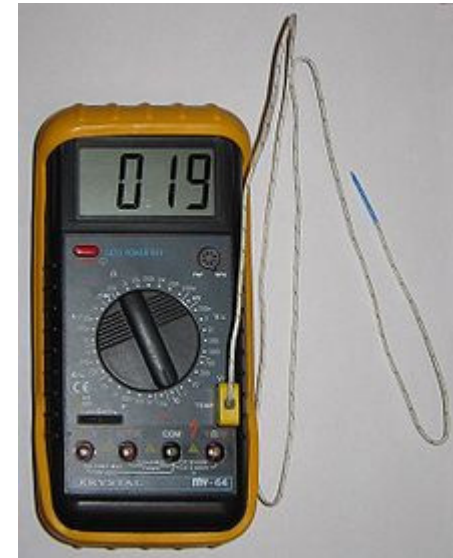
# Thermocouples



inside water heater



inside meat thermometer



connected to multimeter

- Junction of two dissimilar materials, used to measure temperature (based on Seebeck's original experiment)

# Recap: Thermoelectric Modules

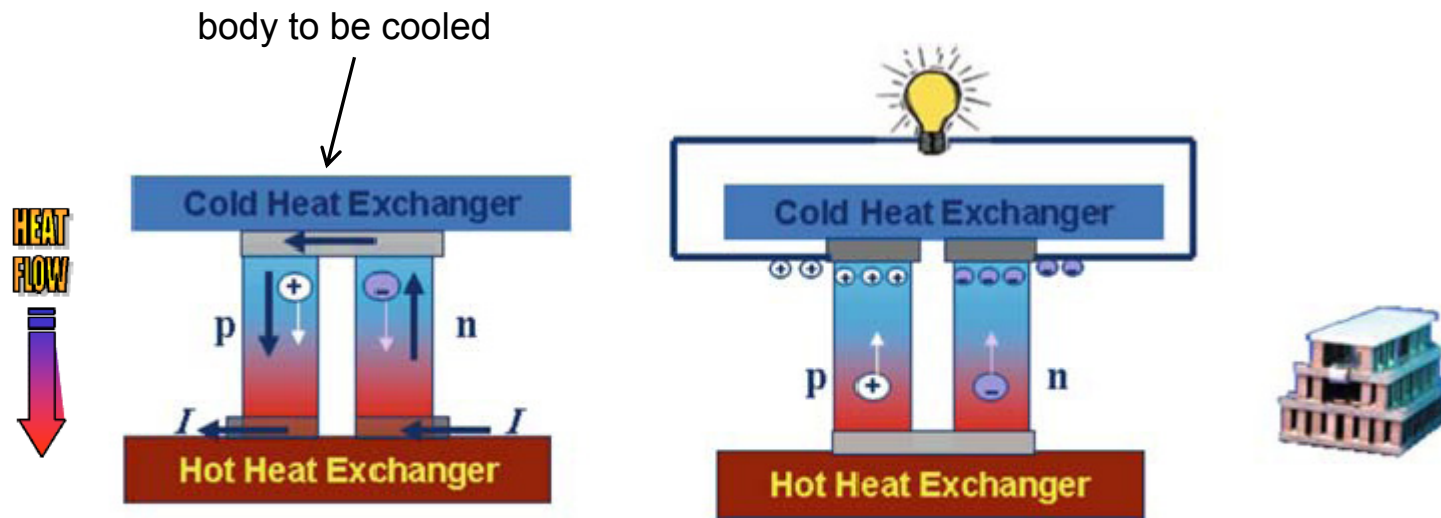
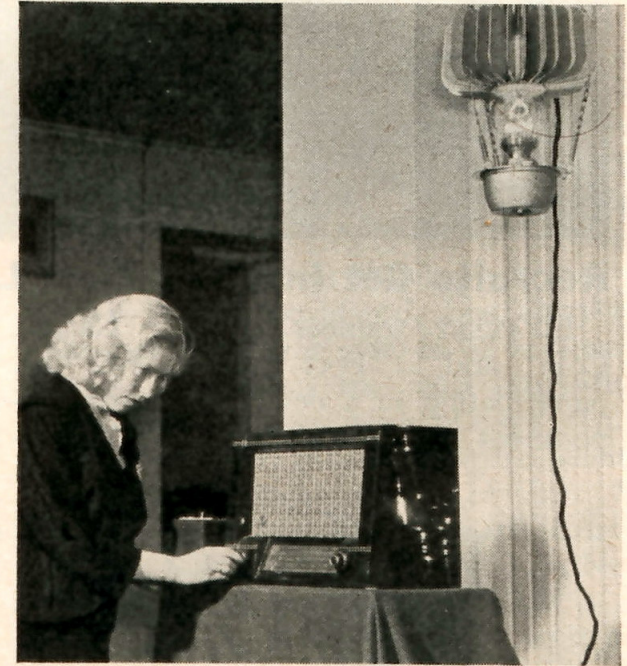


Fig. 9.1 Thermoelectric devices. *Left:* Cooler based on Peltier effect. *Center:* Power generator based on Seebeck effect. *Right:* An actual module

- Use electrons and holes to carry heat and cool a body (e.g. cup holder)
  - Must have good electron and hole conductivity (high  $\sigma$ ,  $S$ )
  - Must block heat “backflow” through (low  $k$ )
- Use temperature gradient (e.g. hot engine to ambient) to generate power
- No moving parts (=quiet and reliable), no freon (=clean)

# More Historical Perspective

- During and after world wars TE research grew, for both cooling and power generation for military and civilian uses
- Some advances could not be shared or were slow (US vs. USSR)
- 1950s: cooling from ambient to 0 °C demonstrated (with  $\text{Bi}_2\text{Te}_3$ )
- Energy harvesting from oil lamp or camp fire to power radios



**Kerosene Radio** Made in Moscow for use in rural areas, this all-wave radio is reportedly powered by the kerosene lamp hanging above it. A group of thermocouples is heated internally to 570 degrees by the flame. Fins cool the outside to about 90 degrees. The temperature differential generates enough current to operate the low-drain receiver. Regular listeners may want fur-lined union suits, though: It works best in a room with open windows.

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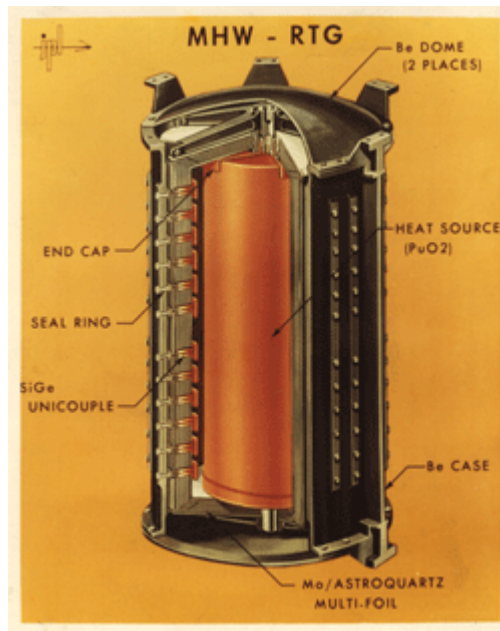


today: the BioLite camp stove  
phone charger (\$130 at REI.com)

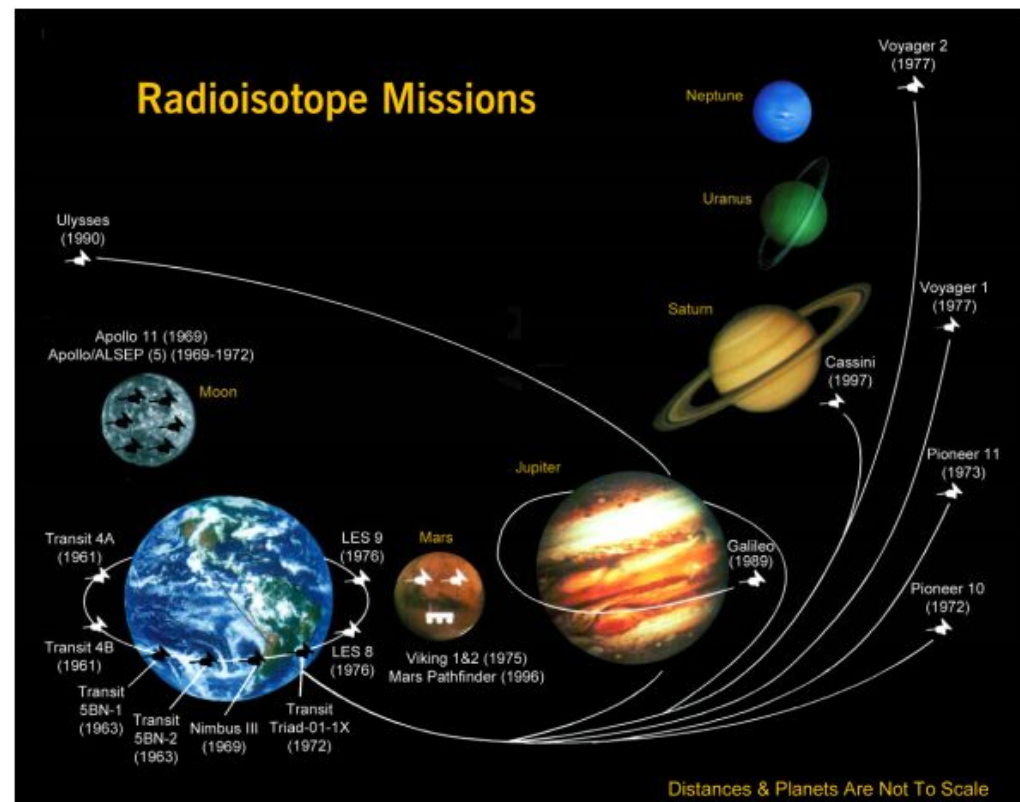


# Radioisotope Thermoelectric Generators (RTGs)

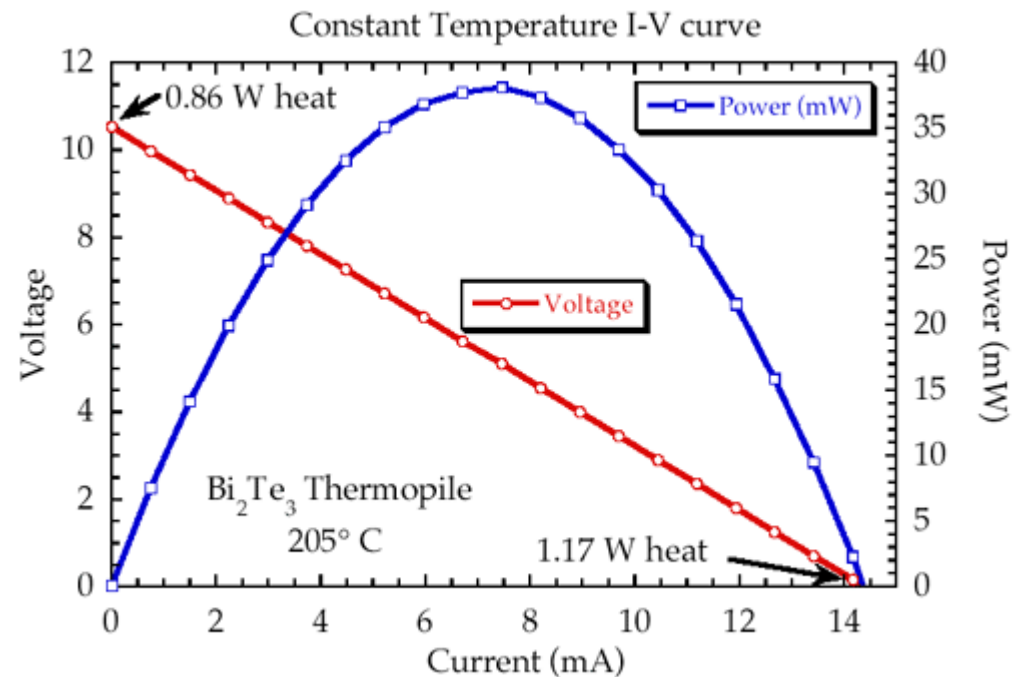
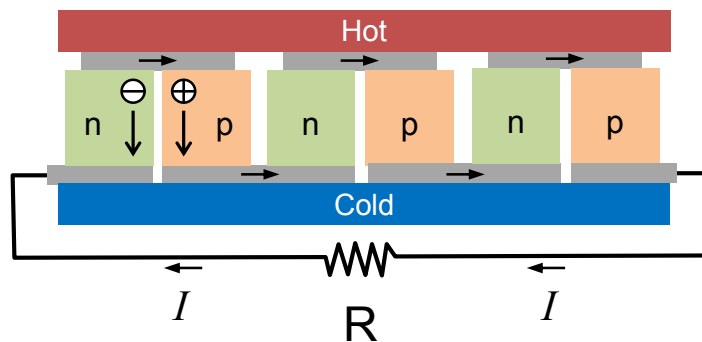
- For remote applications (e.g. lighthouses) and space exploration, electrical power provided by RTG
- RTG converts heat from decaying Pu-238 into electricity
  - Half-life of 90 years and 1 g sufficient for ~0.5 W power
- NASA used RTGs to power Apollo, Voyager, Viking, Curiosity...



RTG for Voyager 1, 2



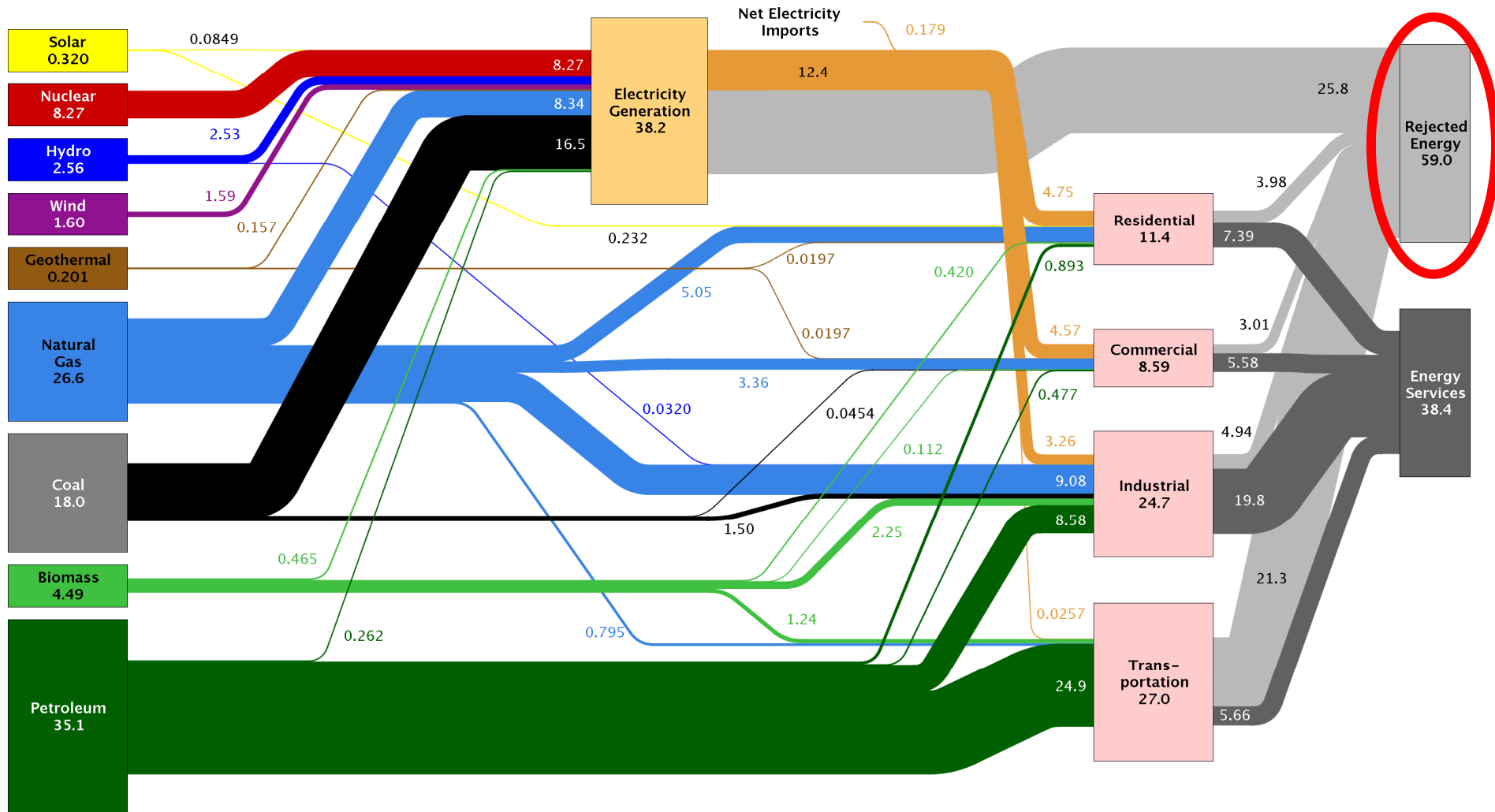
# Current-Voltage-Power Curve of a TEG



- In practice, the internal resistance of TEG and the external load resistance both matter
- Open circuit → max voltage, but no power produced
- High current → voltage is lost on the internal TEG resistance

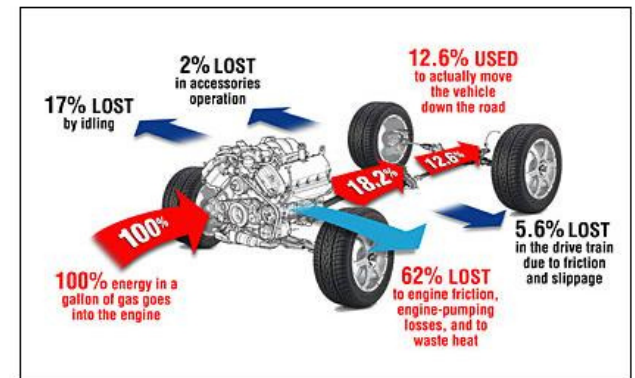
# National Energy Perspective

Estimated U.S. Energy Use in 2013: ~97.4 Quads



# Energy Harvesting from Waste Heat

- Almost everything we do wastes heat
  - Power generation
  - Transportation (engine + friction)
  - Computing
- 15 TW (60%) wasted as heat in the world\*
- Most is “low-grade”  $T \leq 200\text{ }^{\circ}\text{C}$
- Recovering even a few percent would be HUGE, equivalent of several power plants (GW)



thermoelectrics could be a solution

\*Dept. of Energy (2012). **By comparison, ALL data center power consumption world-wide is ~30 GW!**



# Recap: TEs for Refrigeration

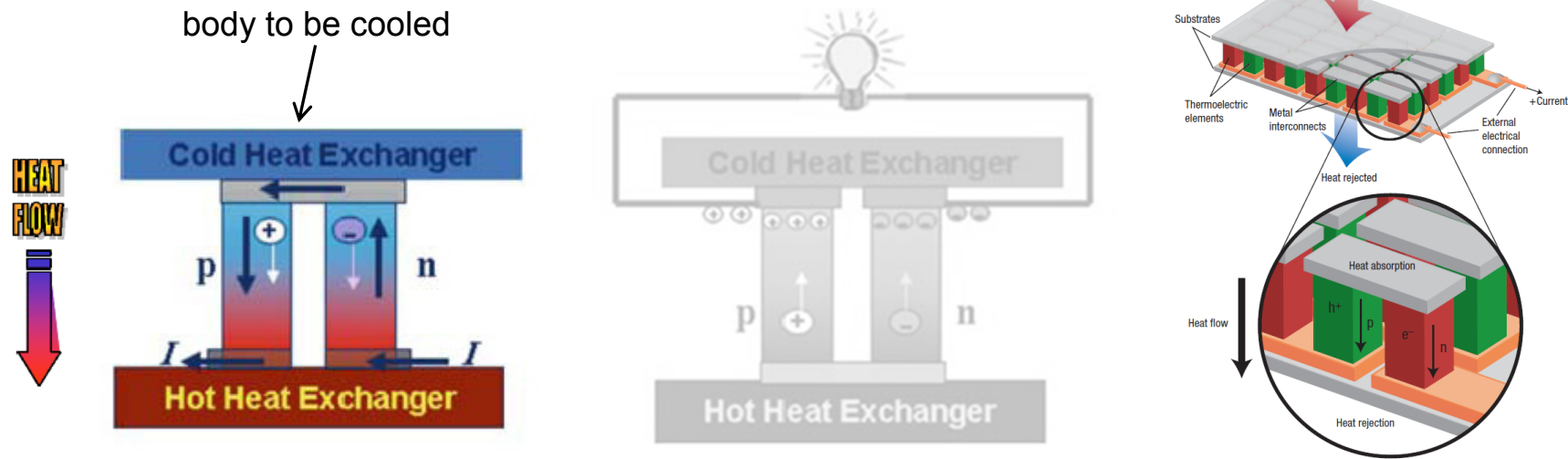


Fig. 9.1 Thermoelectric devices. *Left:* Cooler based on Peltier effect. *Center:* Power generator based on Seebeck effect. *Right:* An actual module (sources: A. Shakouri, G. Snyder)

- Use junction ( $\Delta S$ ) and current to electrically heat or cool
  - Peltier effect:  $Q_{heat,cool} = \pm I \Delta S T$
- **Used in small refrigerators, cooled car seats, cup holders**
- No moving parts (=quiet and reliable), no freon (=clean)



# Recap: TEs for Power Generation

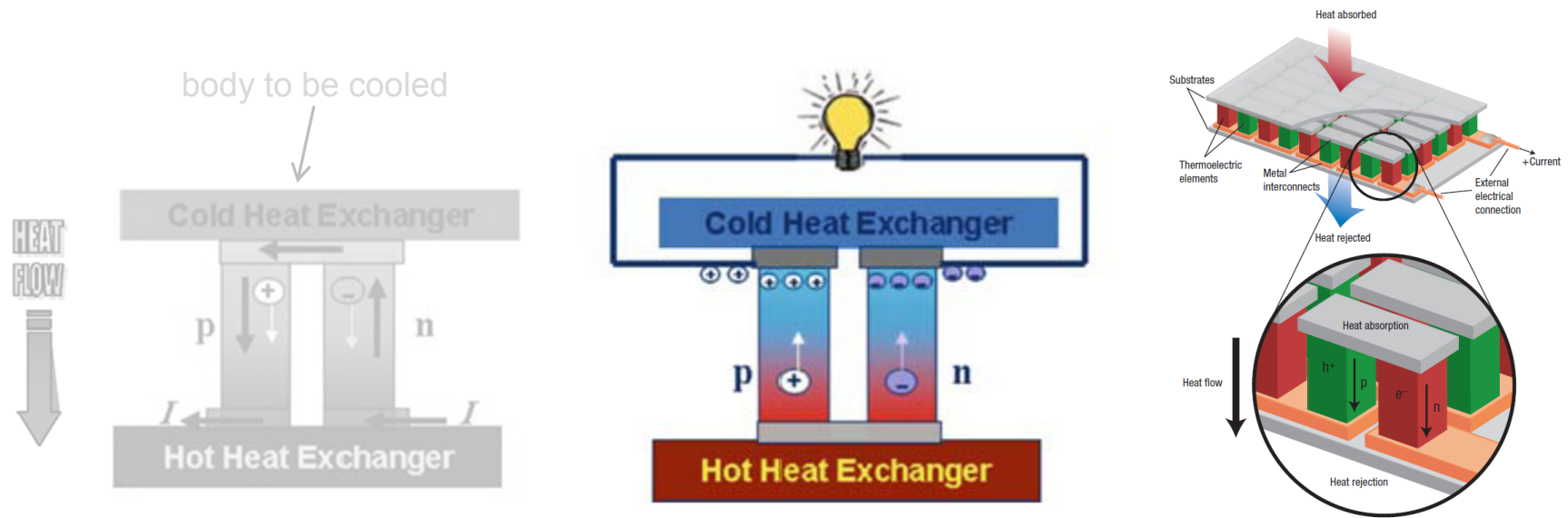


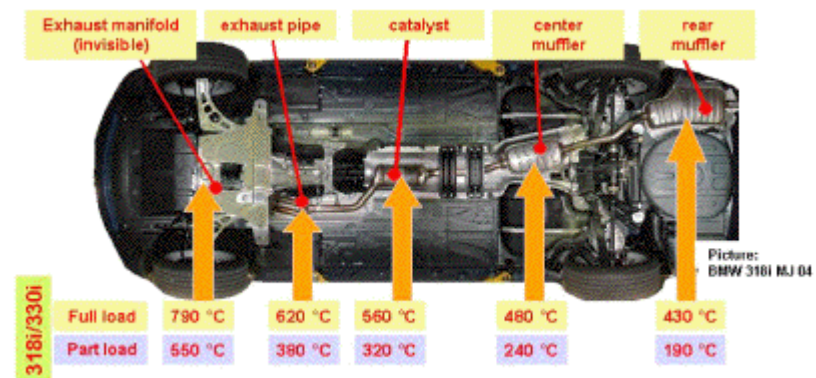
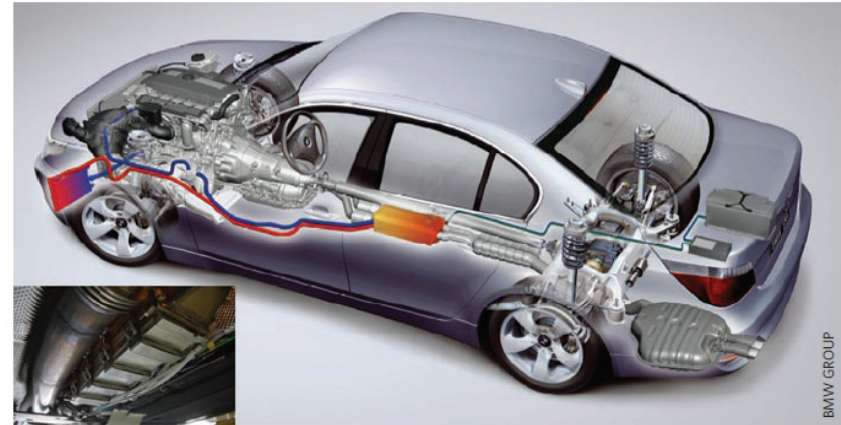
Fig. 9.1 Thermoelectric devices. *Left:* Cooler based on Peltier effect. *Center:* Power generator based on Seebeck effect. *Right:* An actual module (sources: A. Shakouri, G. Snyder)

- Use temperature gradient ( $\Delta T$ ) to generate power
  - Seebeck effect:  $\Delta V \equiv S\Delta T$
- **Used in car engines & exhaust, Mars rover (~100 W)**
- No moving parts (=quiet and reliable), no freon (=clean)



# Ex: Automobile Waste Heat Recovery

- About 75% of energy from combustion lost as heat in exhaust or coolant
- Catalytic converters reach 300-500 C and TEGs can be used to harvest 100s of W
- Small fraction power recovery (consider 1 HP  $\approx$  750 W) but sufficient to power radio or AC and lessen alternator load



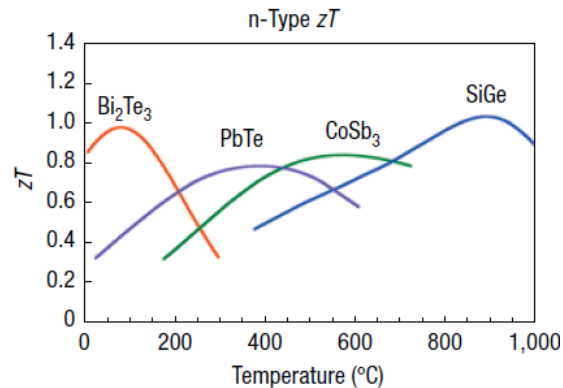
# An Important Perspective

- “Thermoelectric energy conversion will never be as efficient as steam engines. That means thermoelectrics will remain limited to applications served poorly or not at all by existing technology” (Vining, 2009\*)
- However:
  - TEs could play a big role in waste heat recovery
  - Cooling in small size applications (e.g. lasers, seats, cup holders)
  - What matters is not just efficiency (ZT), but cost per Watt
    - *Many groups are looking at polymer TEs even though efficiency is lower than traditional semiconductors, paralleling work in solar cell community*
  - Power generation in communities without power plants and electric grid
    - *TE modules in cooking stoves and solar thermal systems*

\*Vining, “An Inconvenient Truth About TEs” (2009)

# New Materials for Thermal Energy Harvesting

- Traditional thermoelectrics: Bi, Te, Pb → rare, expensive, toxic, brittle

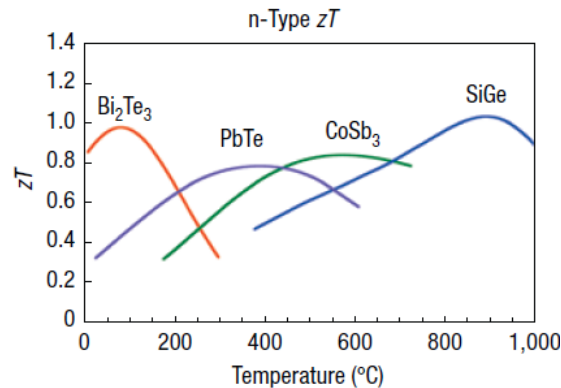


Material	Cost (\$/kg)
$\text{Bi}_2\text{Te}_3$ (bulk)	110
$\text{Bi}_{0.52}\text{Sb}_{1.48}\text{Te}_3$	125
PEDOT:PSS (polymer)	0.34

G. Snyder, *Nature Mat.* (2008); S. Yee *et al.* (2013)

# New Materials for Thermal Energy Harvesting

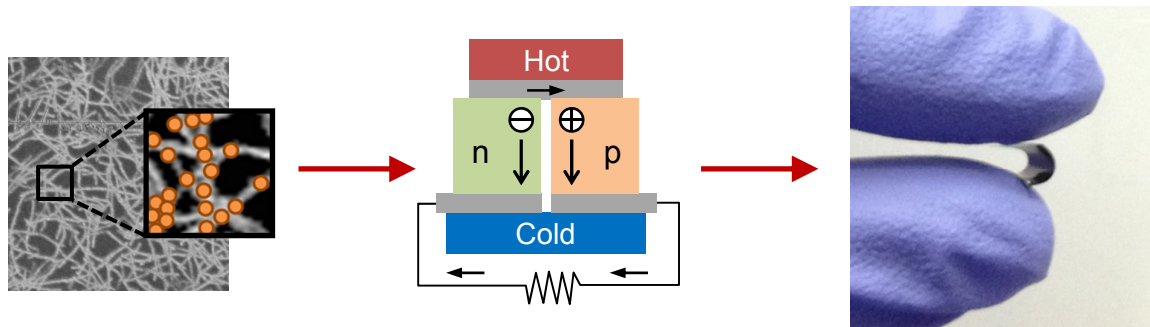
- Traditional thermoelectrics: Bi, Te, Pb → rare, expensive, toxic, brittle



Material	Cost (\$/kg)
$\text{Bi}_2\text{Te}_3$ (bulk)	110
$\text{Bi}_{0.52}\text{Sb}_{1.48}\text{Te}_3$	125
PEDOT:PSS (polymer)	0.34



- Start with **low-cost polymers\*** that already have low  $k$ , high  $\sigma$
- Use nanostructuring (nanotubes, nanowires) to increase  $S$



## Bonus:

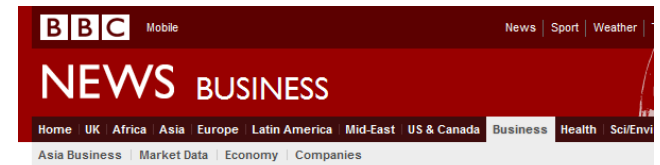
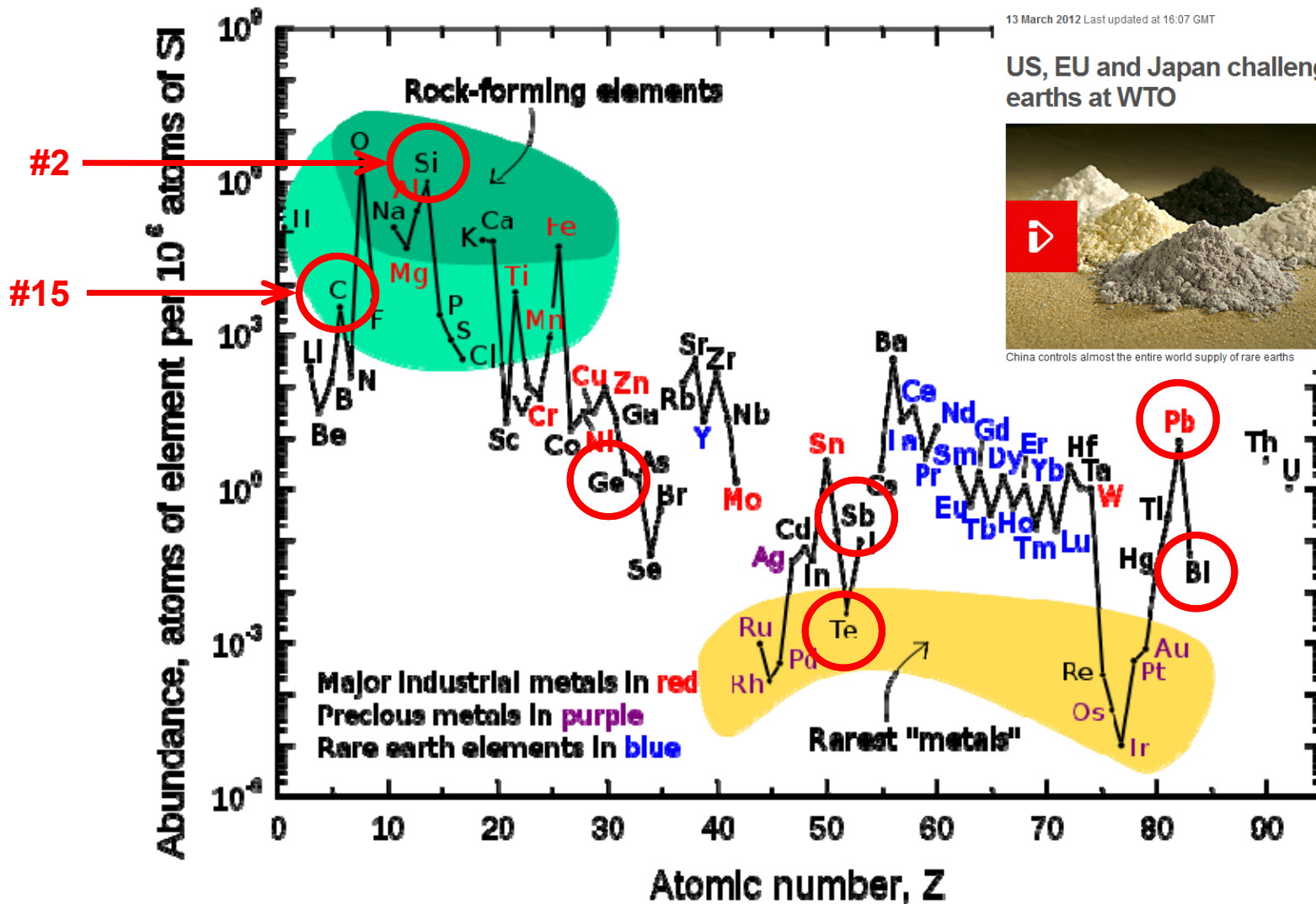
- mechanically flexible
- solution processable

G. Snyder, *Nature Mat.* (2008); S. Yee *et al.* (2013)

\*Berkeley and LBNL (J. Urban and R. Segalman)



# Abundance of Materials



13 March 2012 Last updated at 16:07 GMT

US, EU and Japan challenge China on rare earths at WTO



China controls almost the entire world supply of rare earths

source: <http://pubs.usgs.gov/fs/2002/fs087-02>

# Energy Harvesting From the Human Body

## Power Consumption

desktop PC ~ 100 W

notebook PC ~ 10 W

low-power sensor,  $\mu$ chip ~  $\mu$ W – mW

**human body output at rest ~ 100 W**

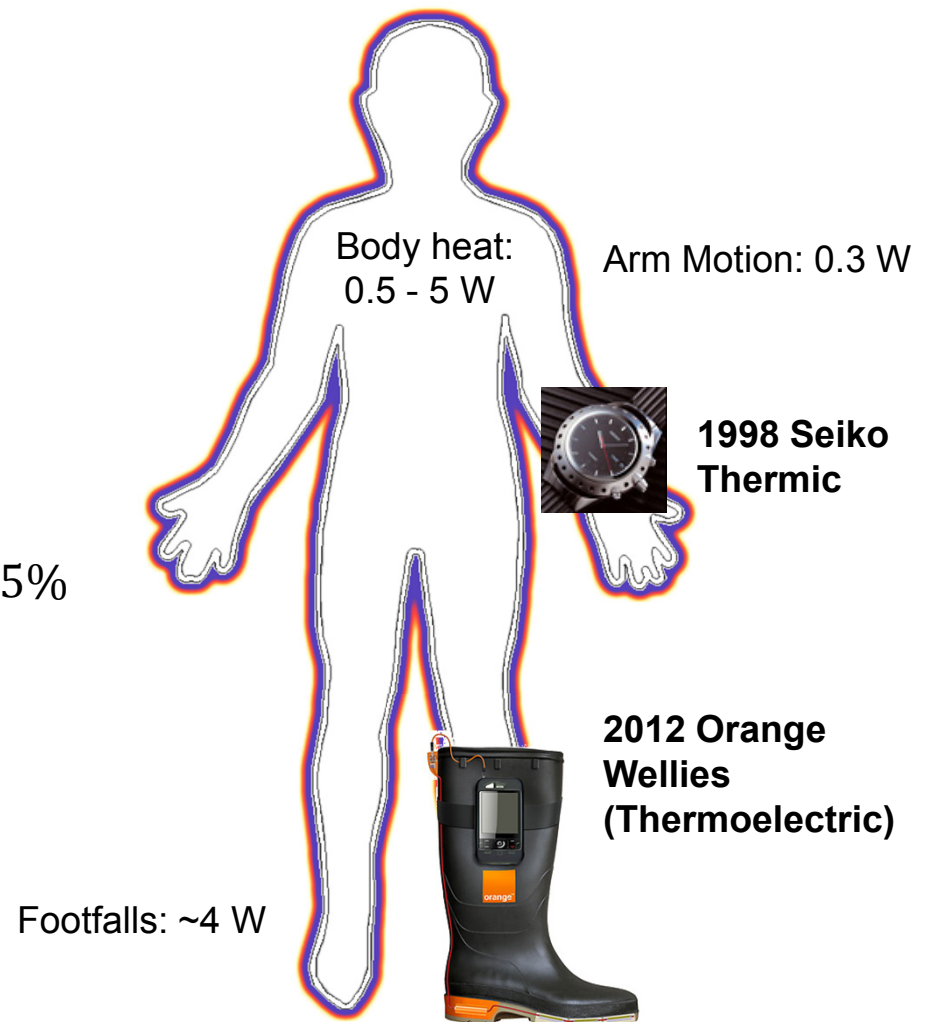
## What's The Upper Limit (Carnot)?

$$\eta_{carnot} = \frac{T_{body} - T_{ambient}}{T_{body}} = \frac{310 - 293 \text{ K}}{310 \text{ K}} \approx 5\%$$

$$\eta_{carnot} \times \eta_{TE} \approx 0.5\%$$

must maximize  $ZT = \frac{S^2 \sigma T}{k_{th}}$

## Usable Power From The Body:

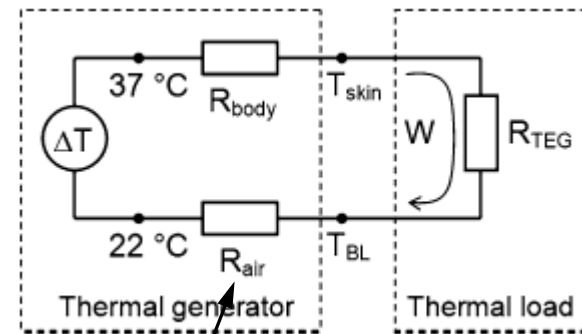
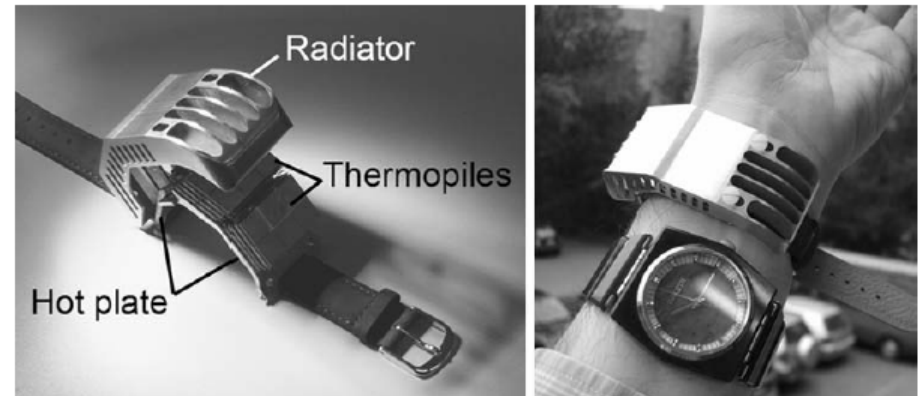


T. Starner, *IBM Systems Journal*, **35** (1996)



# Optimizing Human Energy Harvesting

- Body heat powered watches, boots already demonstrated
- Maximum power harvested is  $\sim 180 \mu\text{W}/\text{cm}^2$  between skin ( $34^\circ\text{C}$ ) and air ( $22^\circ\text{C}$ )
- However, full  $\Delta T = 12^\circ\text{C}$  is not dropped across TEG
- Key is maximizing internal TEG thermal resistance ( $R_{\text{TEG}}$ ) and minimizing TEG-air thermal resistance ( $R_{\text{air}}$ )
- Most also minimize TEG contact resistance (flex-TEG)



parasitics!

source: V. Leonov (2009)

# Outline

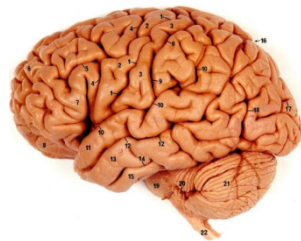
1) Fundamentals

2) Applications

**3) Final Remarks**

# What Motivates Our Research Group

(IBM Watson, *Jeopardy!* champion)



20 Watts

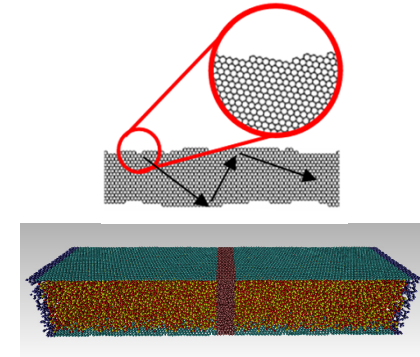
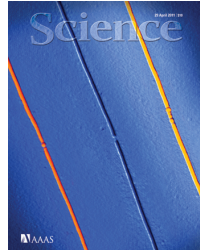
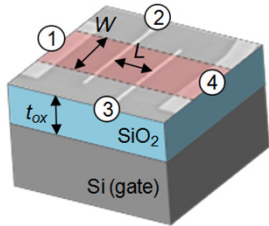


200 kiloWatts

10,000x

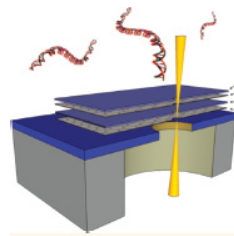
(conventional Moore's Law size scaling can get us ~10x)

# Our Work: Two Sides of the Same Coin



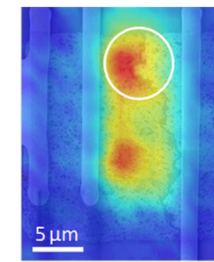
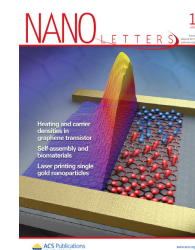
## Lower power at its source

(devices, sensors, circuits)



## Harvest and manage heat

(energy, thermoelectrics)



**fundamental understanding**  
**practical applications**

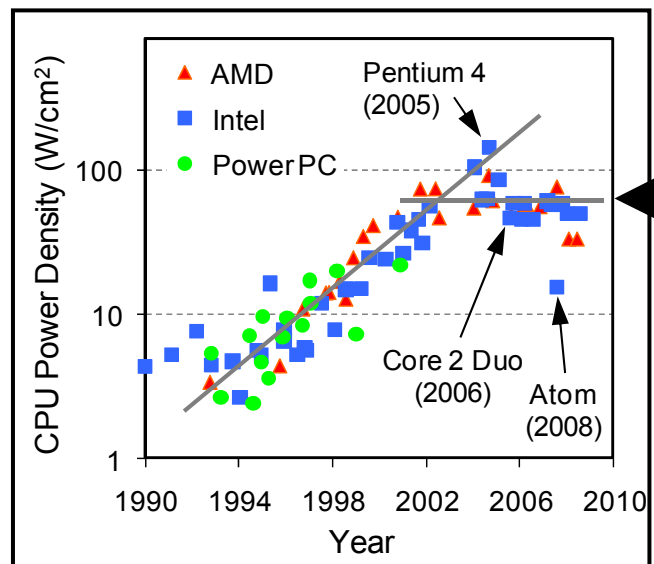


# Pop Lab: Energy and Electronics

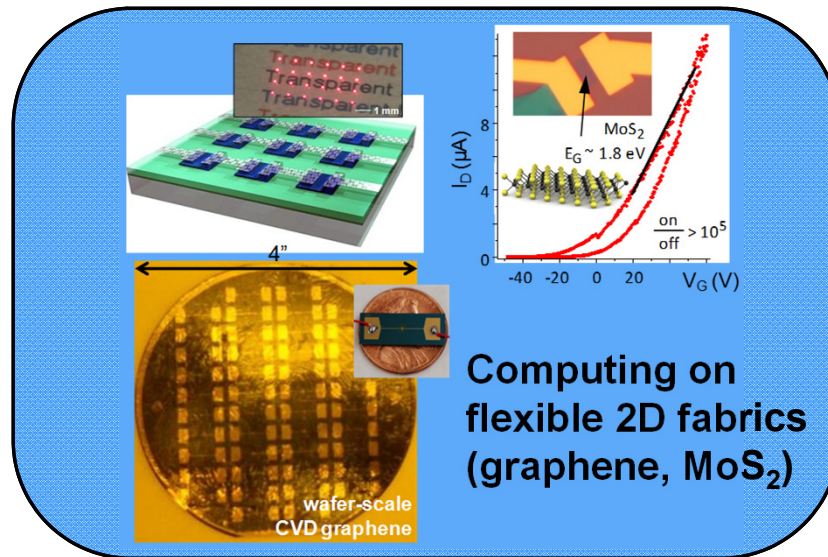
<http://poplab.stanford.edu>

review: E. Pop, *Nano Research* 3, 147 (2010)

new course: EE 323 "Energy in Electronics" in Autumn 2014



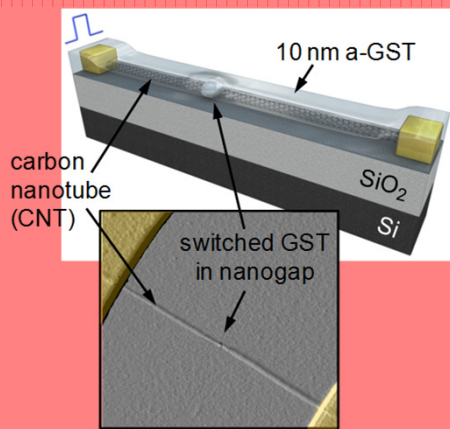
**Electronics,  
limited by  
power & heat  
since 2005!**



**Computing on  
flexible 2D fabrics  
(graphene, MoS<sub>2</sub>)**

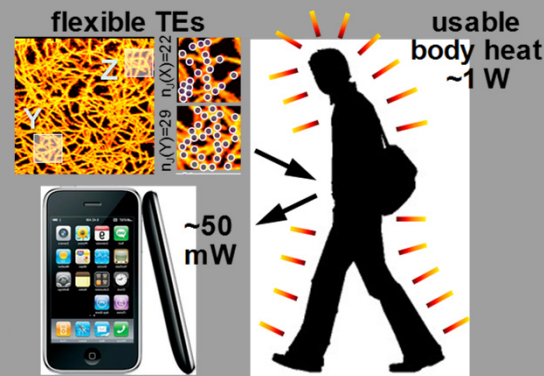
**Energy-efficient  
data storage:**

**100x lower power  
in phase-change  
memory (PCM)**



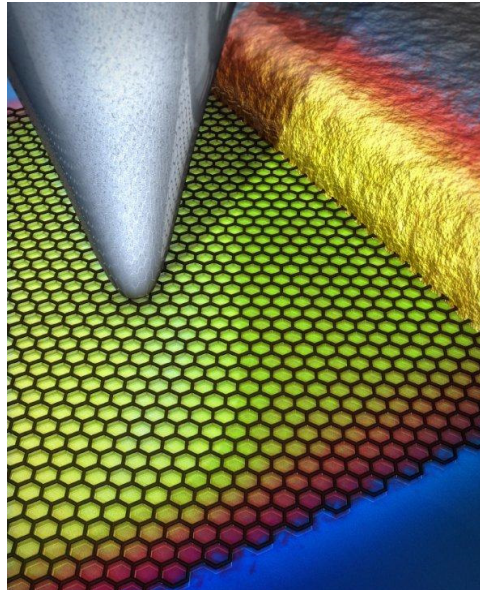
Xiong et al, *Science* (2011)

**Energy harvesting: up to ~1 W from body  
heat using flexible thermoelectrics (TE)**

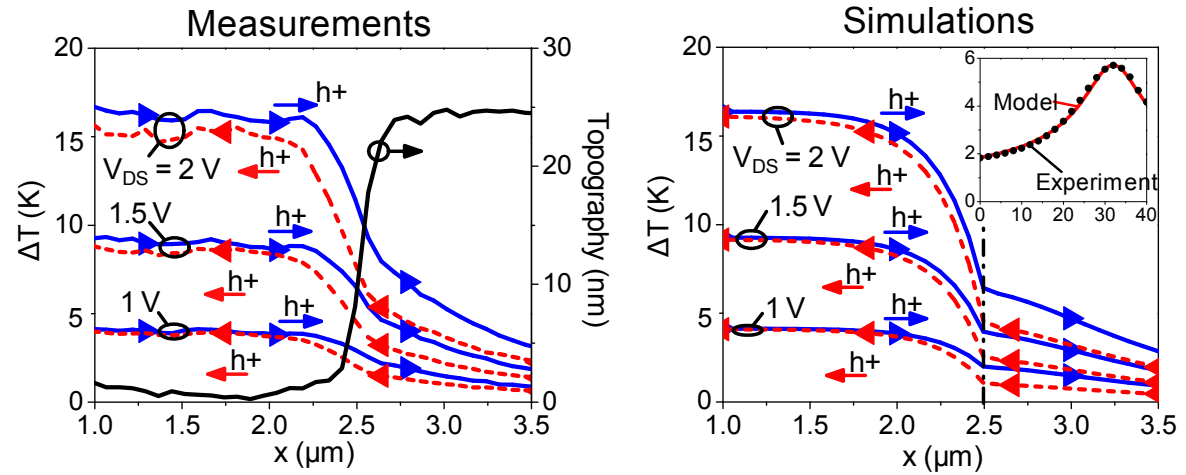
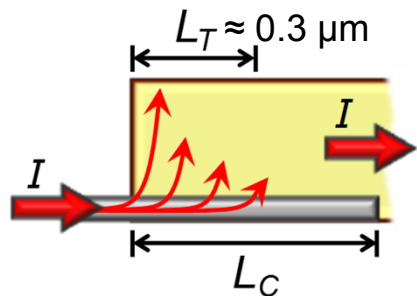


# Thermoelectric Effects at Nanoscale Contacts

K. Grosse, M.-H. Bae, F. Lian, E. Pop, W. King, *Nature Nano* 6, 287 (2011)



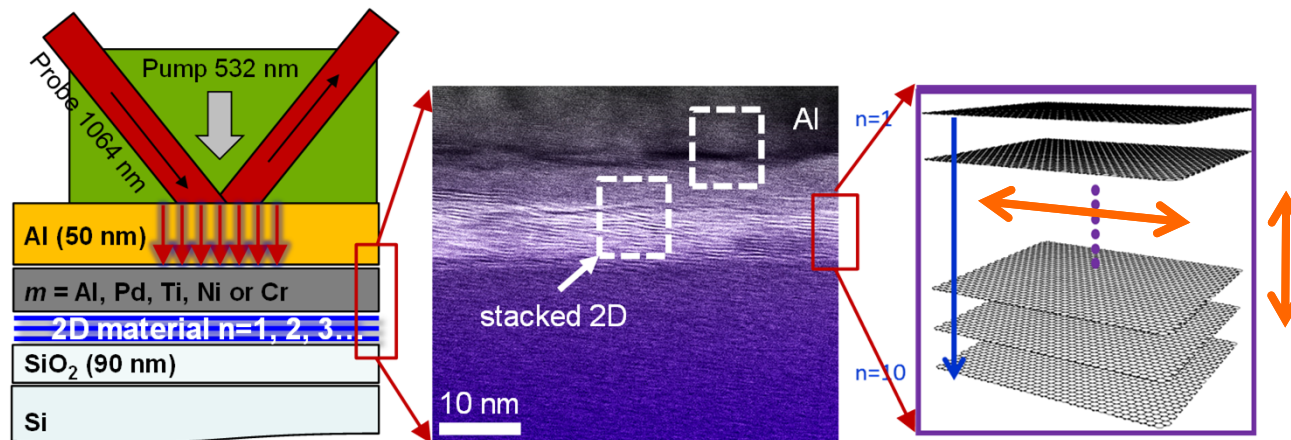
scanning Joule expansion microscopy (SJEM)



- AFM-based thermometry (SJEM)
- Contact temperature due to:
  - Current crowding (CC) } 2/3
  - **Thermoelectric effect (TE)** } 1/3
- Some 2D materials have large thermopower  $S$ 
  - Engineer cooling at device contacts?
  - Design built-in TE coolers?

# Looking Ahead: Unusual 2D Materials

- **Large in-plane** thermal conductivity of graphene ( $>1000$  W/m/K)
- **Ultra-low cross-plane** thermal conductivity of layered  $\text{WSe}_2$  ( $<0.1$  W/m/K)
  - Lower than plastics and **comparable to air**\*
- Huge thermal anisotropy in all layered 2D materials ( $>10$ - $100\times$ )\*\*



- **Large thermopower** in some 2D materials ( $\sim 0.5$  mV/K)
- Favorable properties for thermoelectrics

\*C. Chiritescu et al., *Science* (2007)

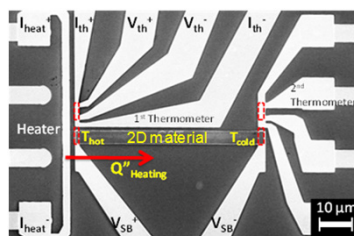
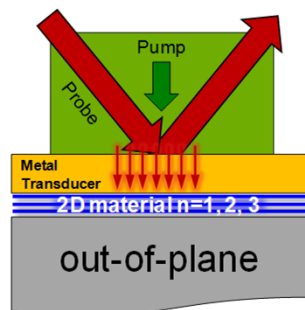
\*\*E. Pop, V. Varshney, A. Roy, *MRS Bulletin* (2012)

\*\*D. Estrada, Z. Li, F. Lian, [...], E. Pop, *in preparation* (2014)

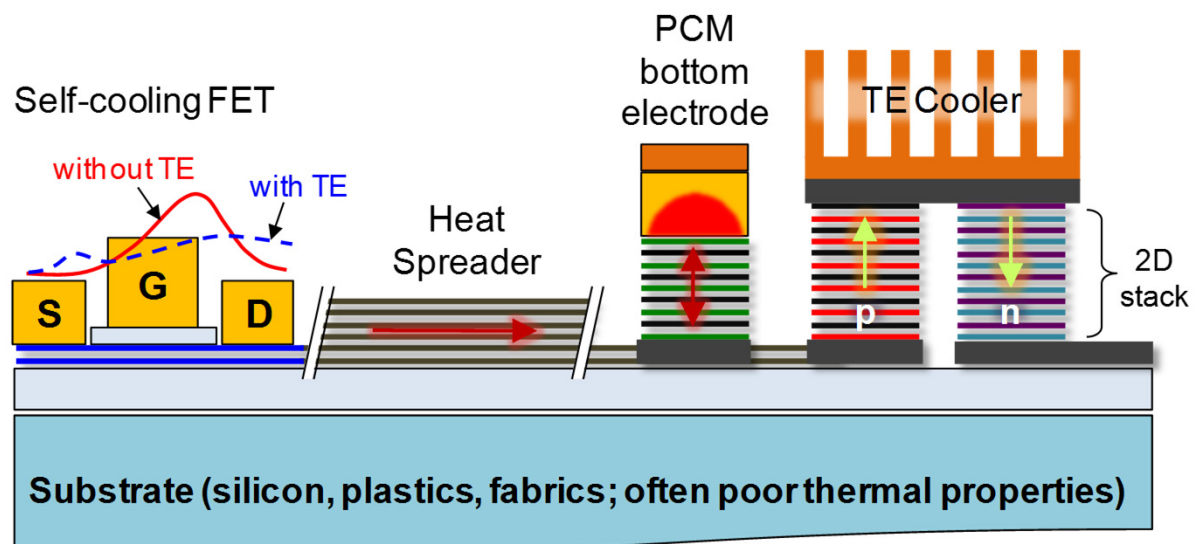
# Looking Ahead: Future Opportunities

## Could we:

- Exploit **anisotropy** for low-power electronics? (e.g. phase-change memory)
- Separate thermal and electrical flow? (thermal transistor)
- Design **electronics with built-in thermoelectric cooling**?
- Achieve transparent heat spreaders and flexible thermoelectrics?

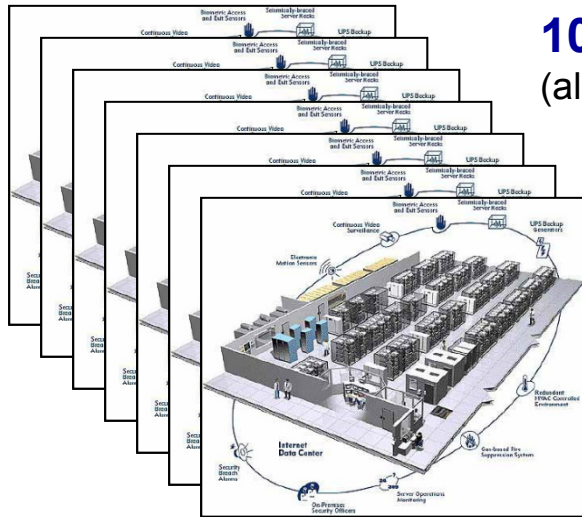


in-plane

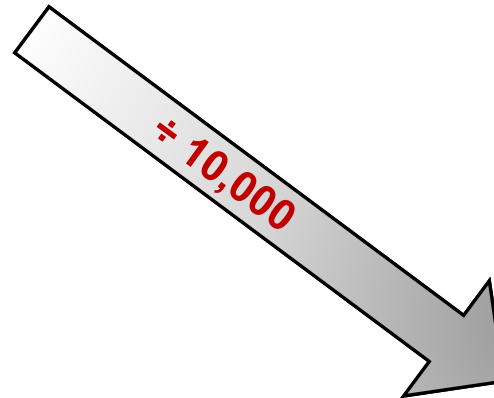




# What Is 10,000x Electrical Power Reduction?

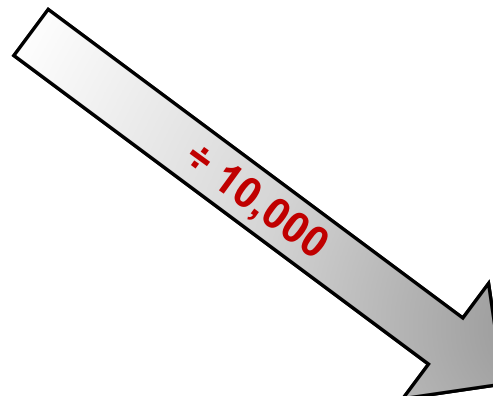


**10 GW**  
(all data centers in US)



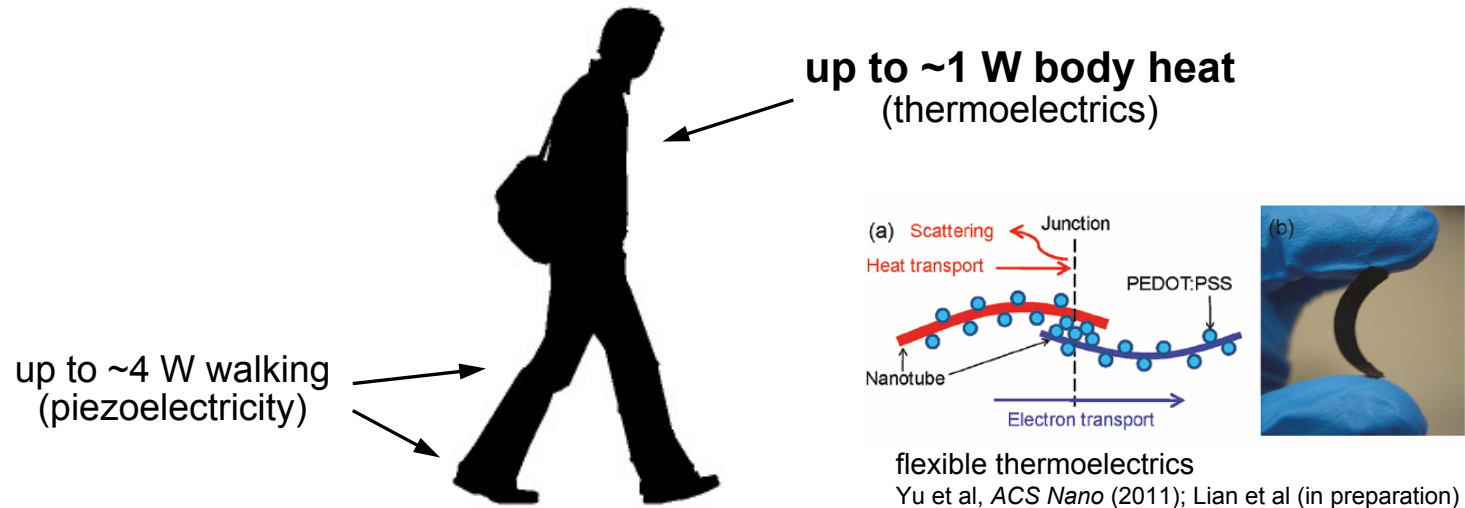
**1 MW**  
(2 Ferrari F430)  
(solar power from 1 parking lot)

**50 mW**  
(average)



**5  $\mu$ W**  
(powered by body heat)

# Low Power Devices + Energy Harvesting



**50 mW**  
(average)



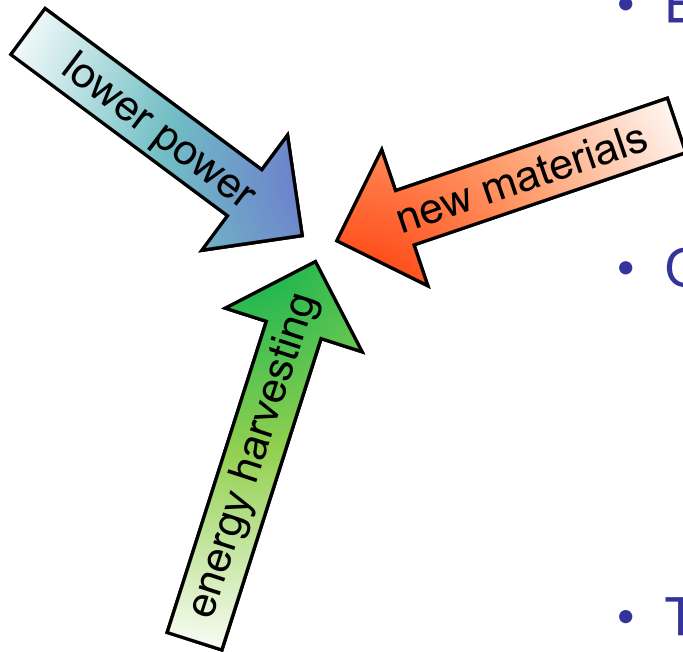
meet in  
the middle?

$\div 10,000$



**5  $\mu$ W**  
(powered by body heat)

# Summary



- Moore's Law  $\sim 10x$  → slowing down
- Energy scaling & harvesting  $\sim 10^4x$  → exciting
- Opportunity for convergence of:
  - Low power electronics
  - **Energy harvesting**
  - Novel nanomaterials
- Towards fundamental limits of energy use (up to 10,000x improvements may be possible)

MUCH room for optimization of energy dissipation, use, and harvesting from the "atomic" level

# Key References

- <http://www.thermoelectrics.caltech.edu> (web tutorial)
- <http://core.kmi.open.ac.uk/download/pdf/11784960.pdf> (historical)
- <http://www.crcnetbase.com/isbn/978-0-8493-0146-9> (CRC Handbook of TEs)
- <http://dx.doi.org/10.1002/adma.201000839> (nanostructured TEs)
- <http://dx.doi.org/10.1146/annurev-matsci-062910-100445> (recent developments)
- <http://dx.doi.org/10.1038/nmat2361> (inconvenient truth)
- <http://dx.doi.org/10.1039/C3EE41504J> (\$/W metrics)
- <http://dx.doi.org/10.1016/j.rser.2013.12.030> (material and manufacturing costs)
- <http://dx.doi.org/10.1063/1.4803172> (nanoscale Peltier in data storage)
- <http://dx.doi.org/10.1007/s11664-008-0638-6> (wearable TEGs)